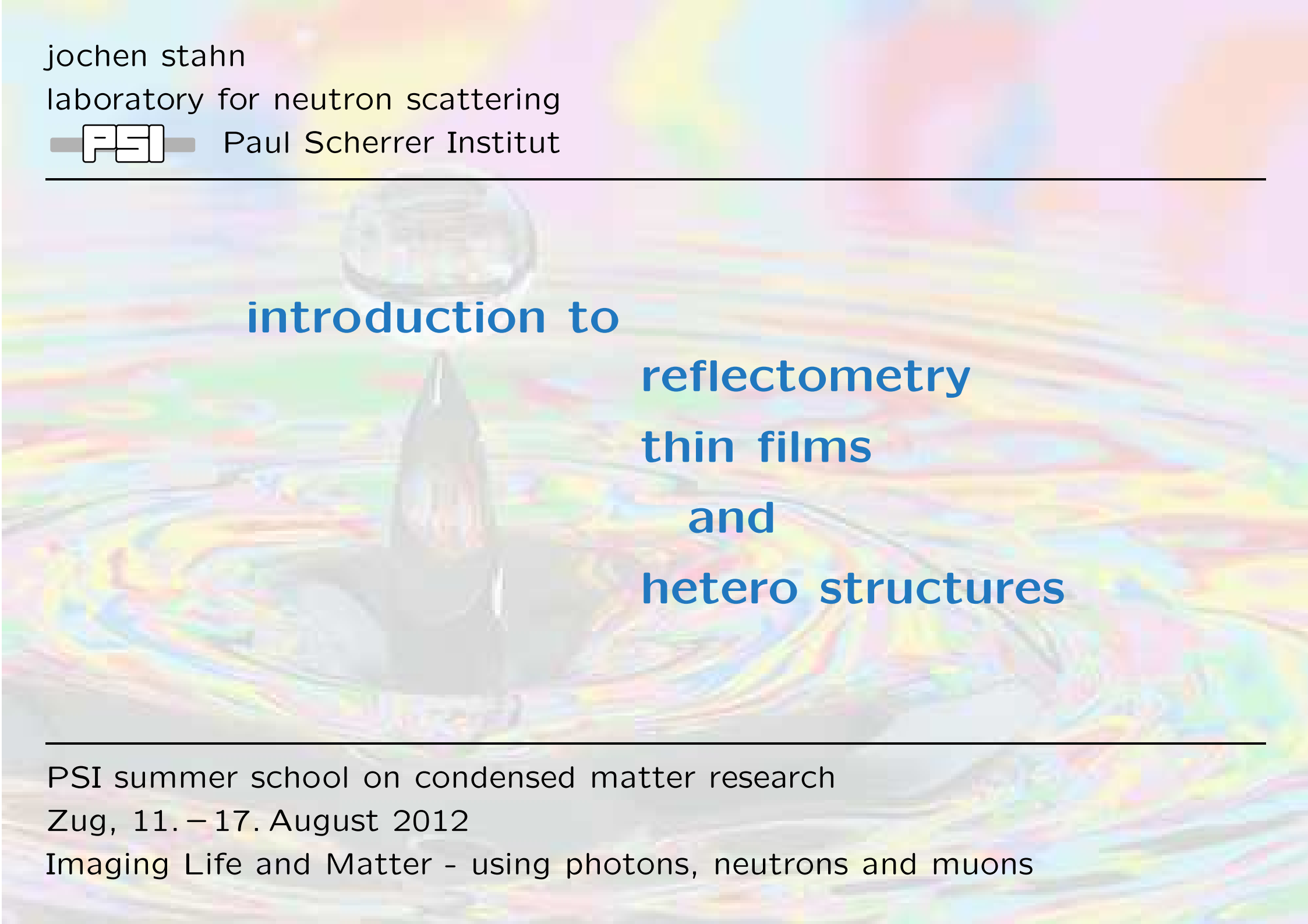


jochen stahn

laboratory for neutron scattering



Paul Scherrer Institut

The background of the slide is a grayscale image of a neutron interferometer. It shows a central vertical column with a sharp tip, surrounded by a complex network of horizontal and vertical lines, representing the optical paths of neutrons. The image is slightly blurred, giving it a scientific, artistic feel.

introduction to reflectometry thin films and hetero structures

PSI summer school on condensed matter research

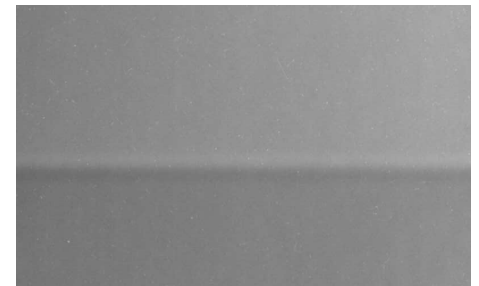
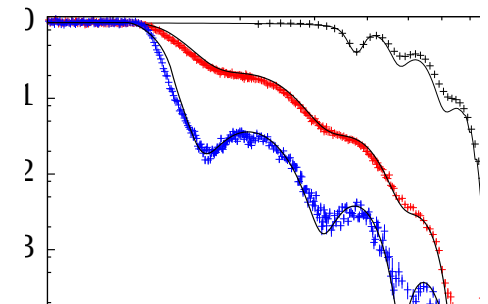
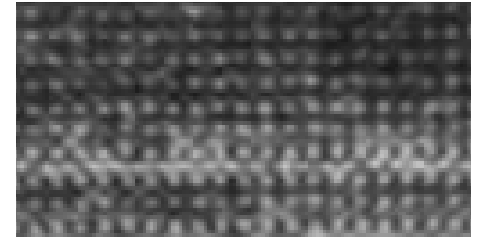
Zug, 11. – 17. August 2012

Imaging Life and Matter - using photons, neutrons and muons

outline

- heterostructures
 - magnetic layers
 - membrane systems
- reflectometry
 - (few formulae)
- ... derivation
 - (lots of formulae)
- experimental examples
 - Fe/Si
 - FeSi/GaAs interfaces
 - bio-membrane
- relevance for imaging
 - YES, there is some!

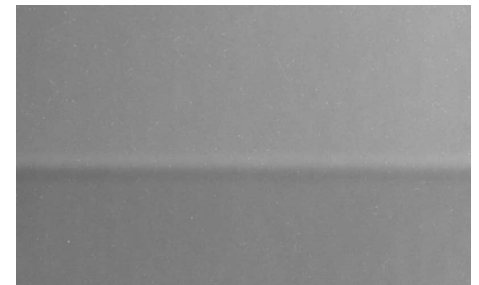
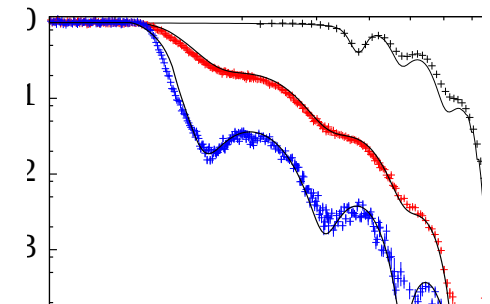
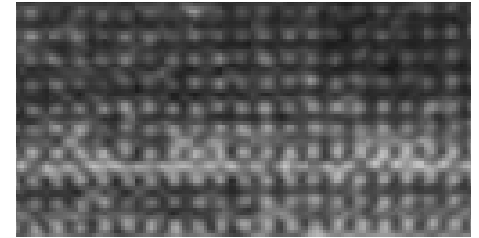
reflectometry 1



outline

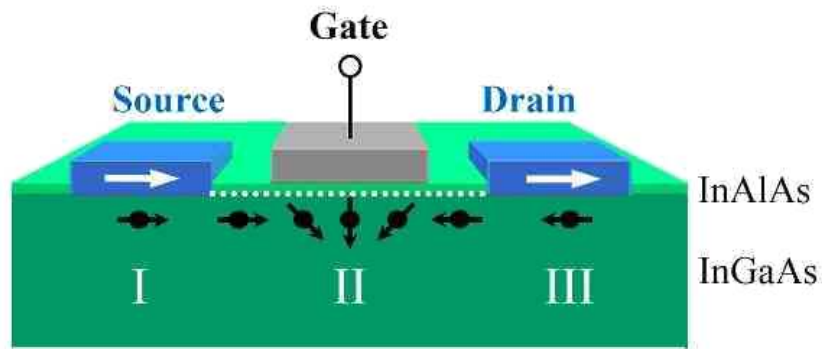
- heterostructures
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reflectometry 2



... the damn magnetically dead layers ...

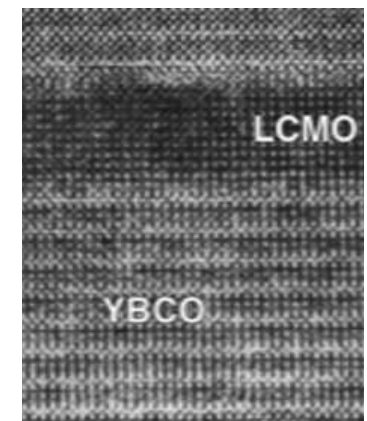
- down-scaling $\Rightarrow$ thin magnetic films
e.g. magnetic data storage



- spin polarised electron injection
e.g. spin-injection in a spin-transistor

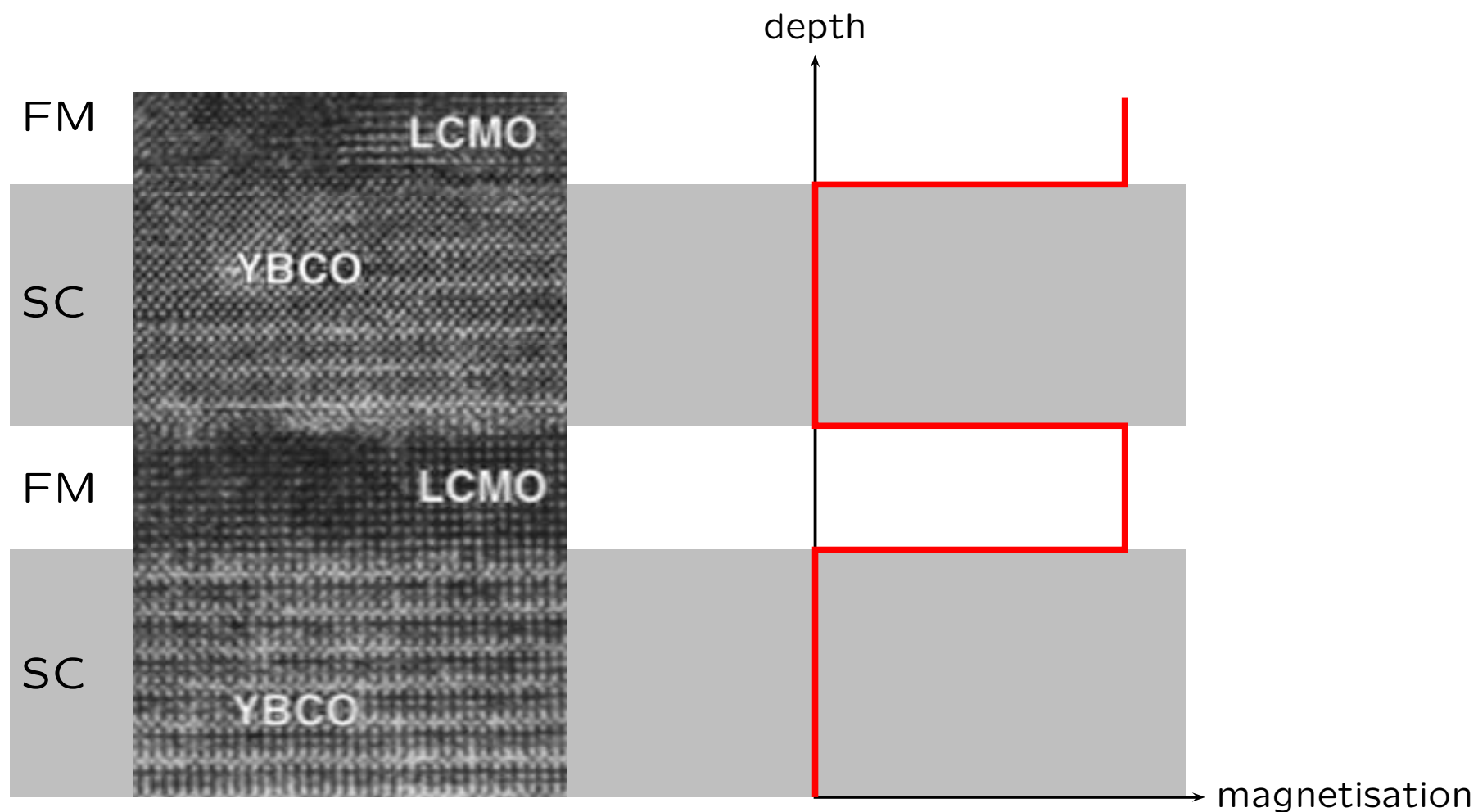


- conflicting properties at interfaces
e.g. interface $\frac{\text{ferro} - \text{magnet}}{\text{superconductor}}$



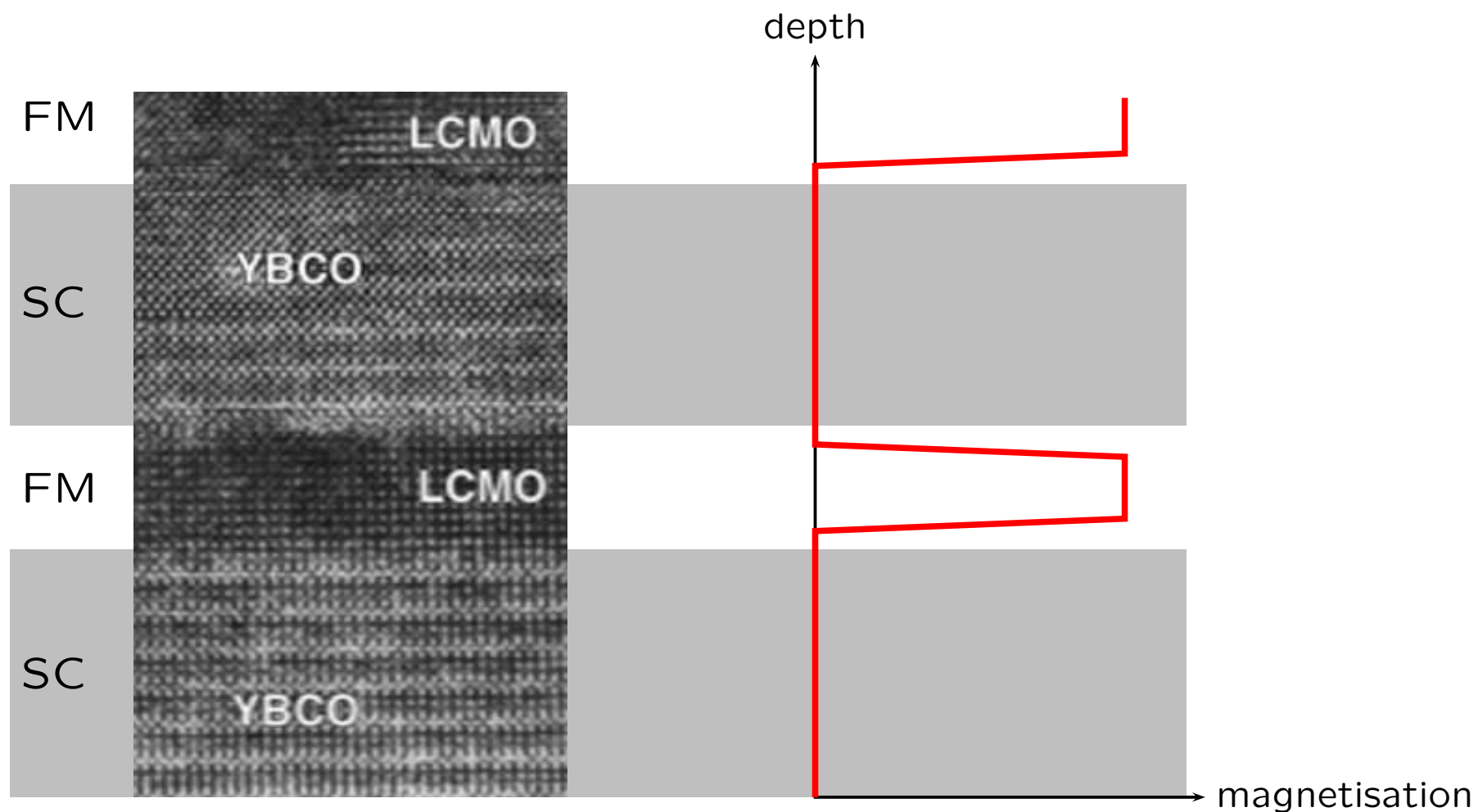
conflict of interests at superconductor / ferromagnet interfaces

(1) no interaction:



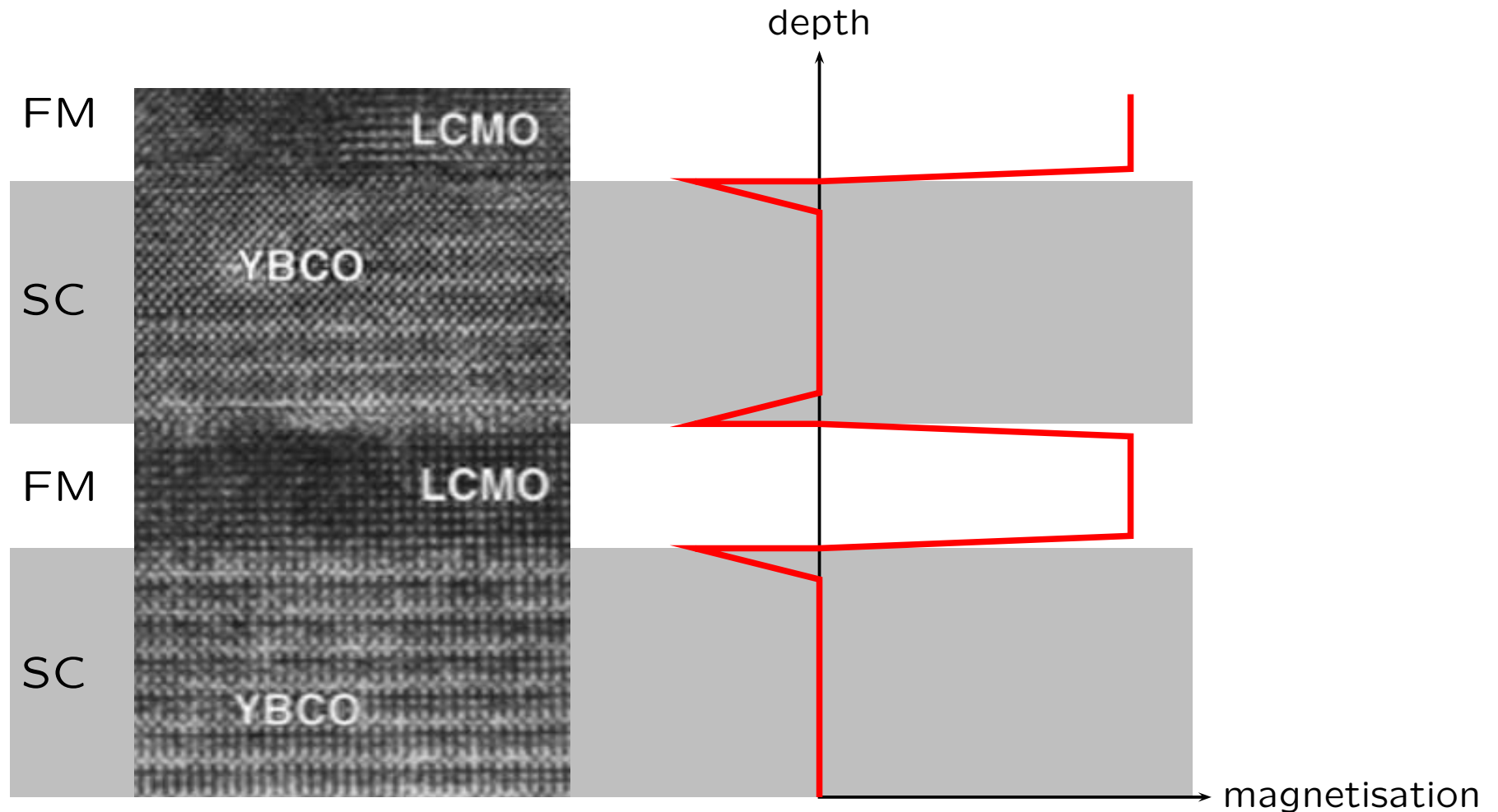
conflict of interests at superconductor / ferromagnet interfaces

(2) suppression of magnetism:



conflict of interests at superconductor / ferromagnet interfaces

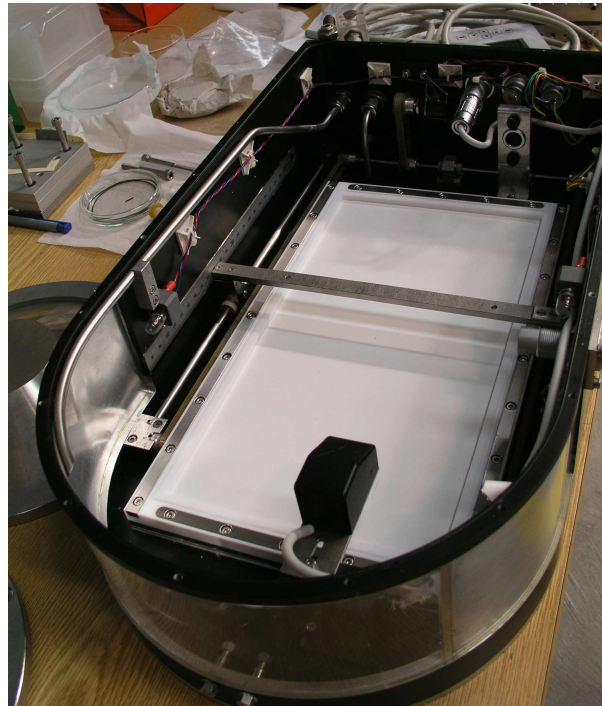
(3) reality: induced magnetism within SC!



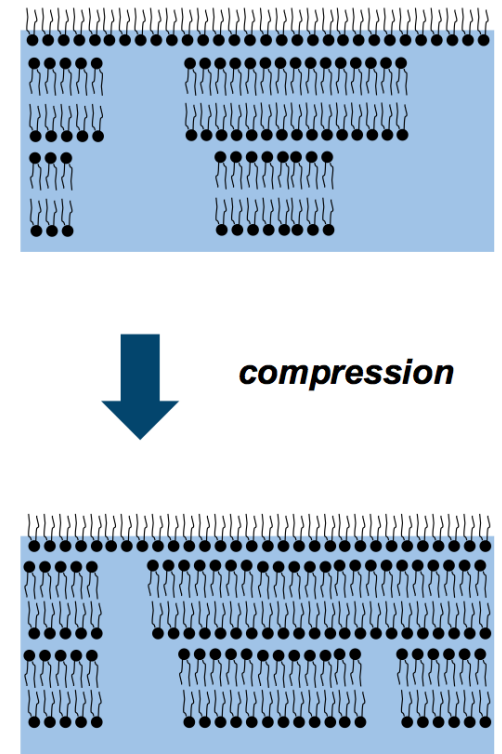
Habermaier, Physica C 364, 298 (2001); Holden, PRB 69, 064505 (2004);
Stahn, PRB 71, 140509(R) (2005)

compression of self-organising polyglycerol-ester films

model-system for
foams used for stabilising food products
e.g. yogurt



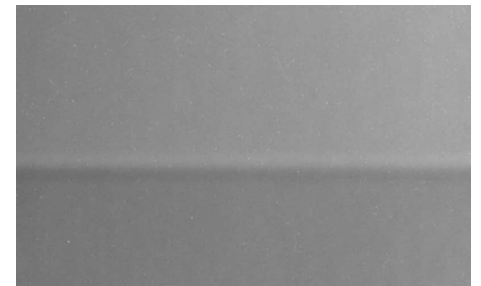
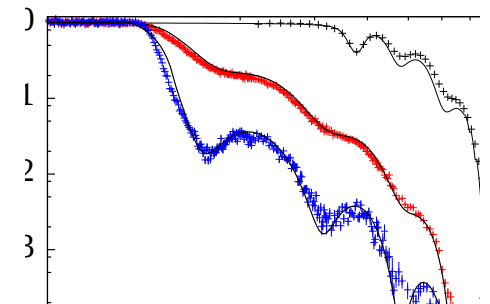
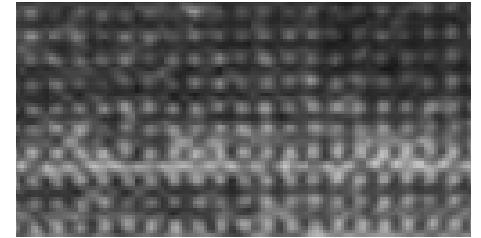
trough to investigate
membranes at the
liquid/air interface



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reflectometry 8





flat surfaces partly reflect light

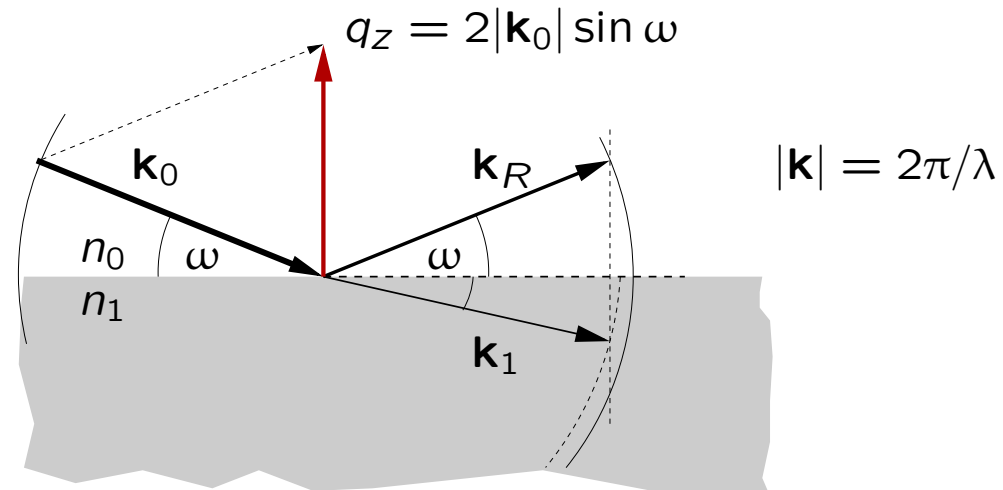
→ picture of the boot

some media also transmit light

→ ground below the water

parallel interfaces

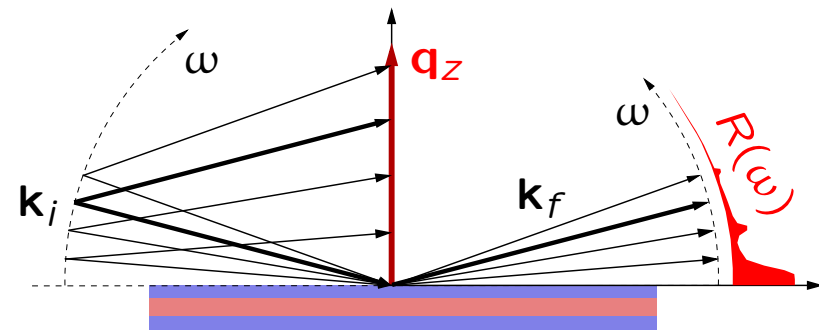
→ colourful soap bubbles



$$R = R(q_z) = R(\lambda, \omega) \quad q_z = 4\pi \frac{\sin \omega}{\lambda}$$

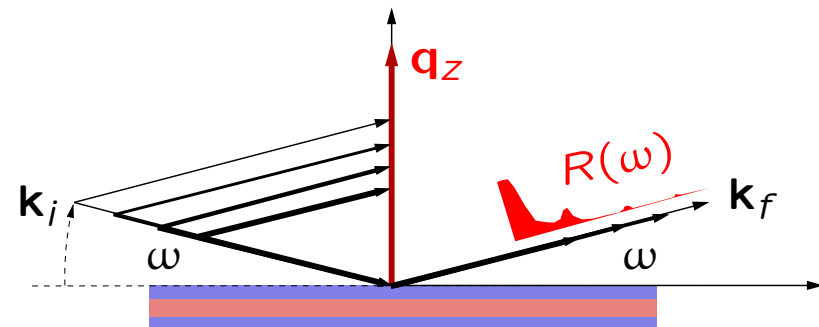
angle-dispersive set-up

variation of ω with fixed λ
detection under 2ω



energy-dispersive set-up

variation of λ with fixed ω
detection via time-of-flight

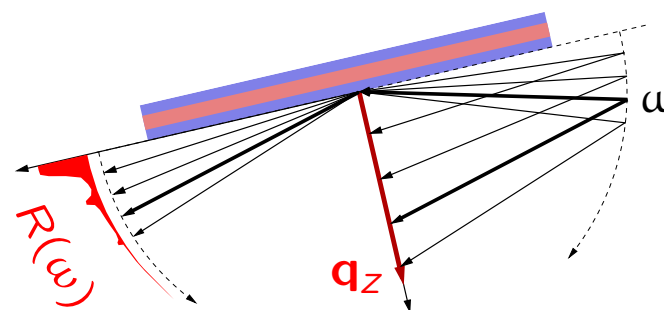
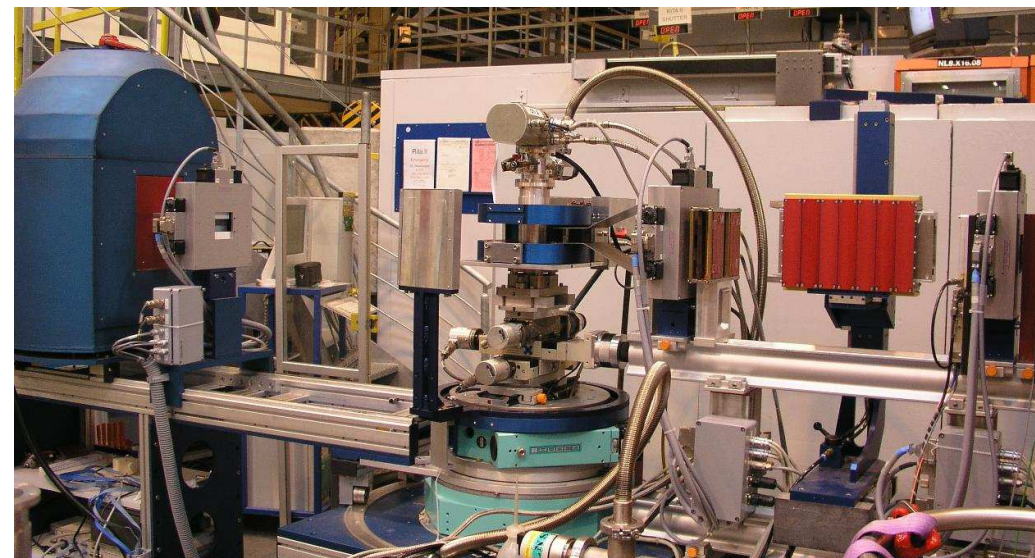
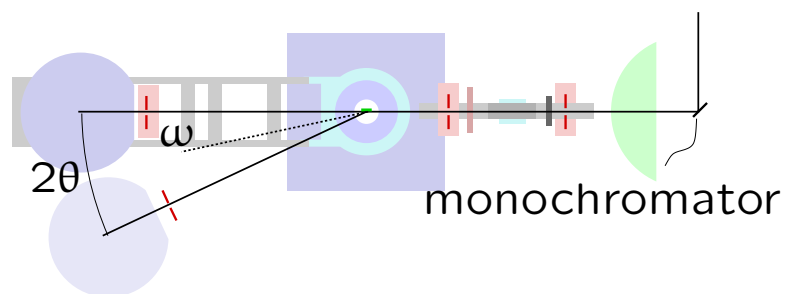
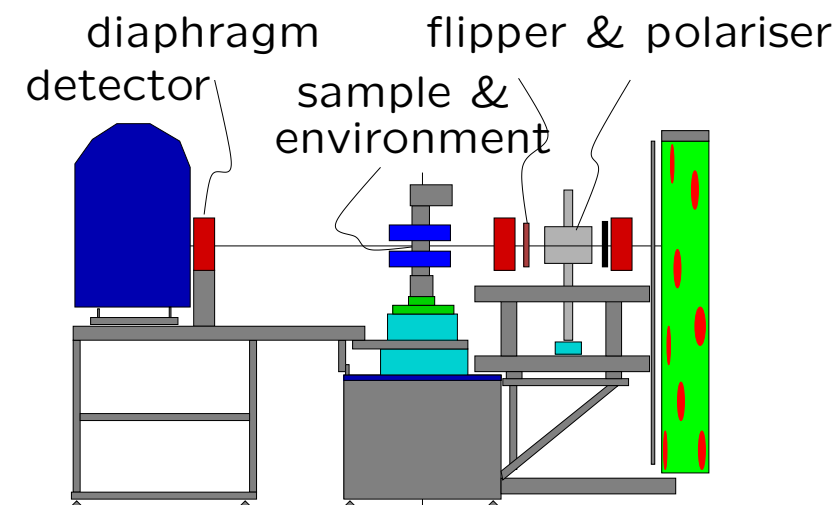


angle-dispersive set-up

reflectometry 11

neutron reflectometer

instrument: Morpheus at SINQ



sample environment

cooling with a
closed cycle refrigerator

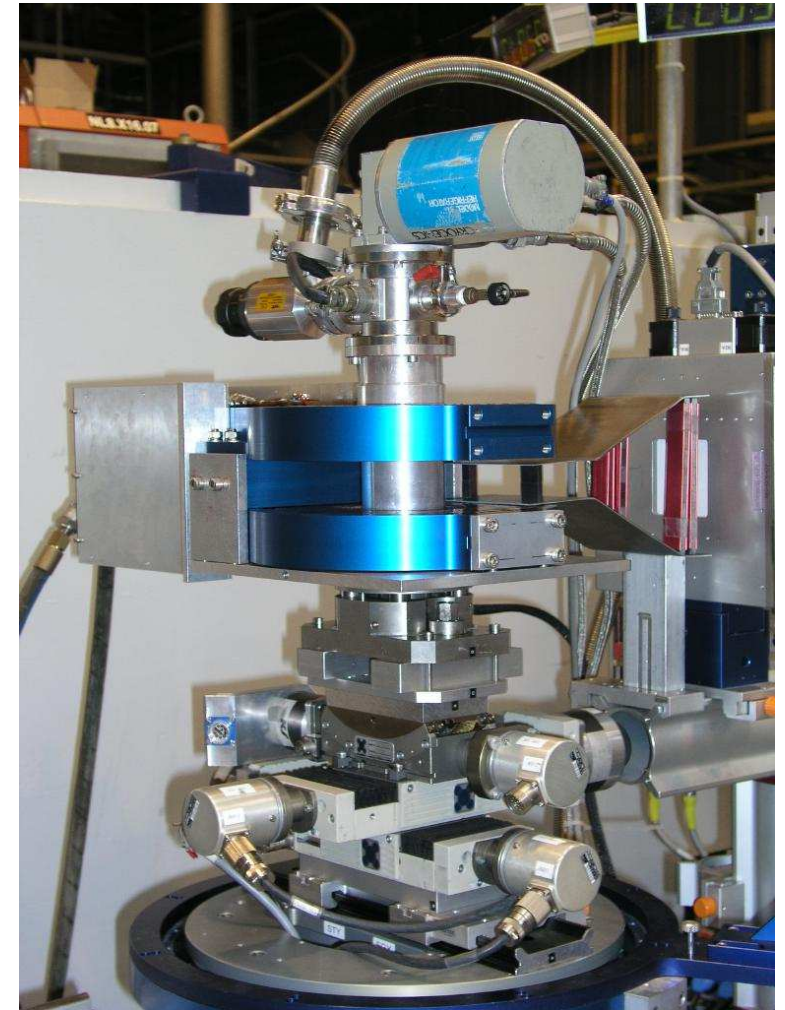
$$8\text{ K} < T < 300\text{ K}$$

application of an external magnetic field with
Helmholtz coils $-1000\text{ Oe} < H < 1000\text{ Oe}$

and sample



reflectometry 12



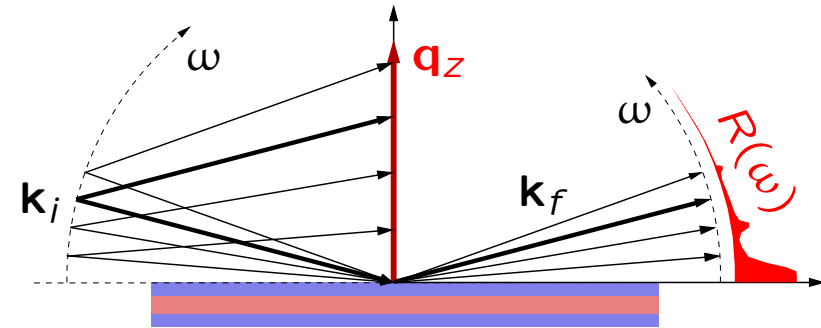
tilt- and
translation stages
for alignment

typical quantities:

angular range $0^\circ \dots 10^\circ$

λ range $3 \text{ \AA} \dots 15 \text{ \AA}$

measurement time $10 \text{ min} \dots 12 \text{ h}$

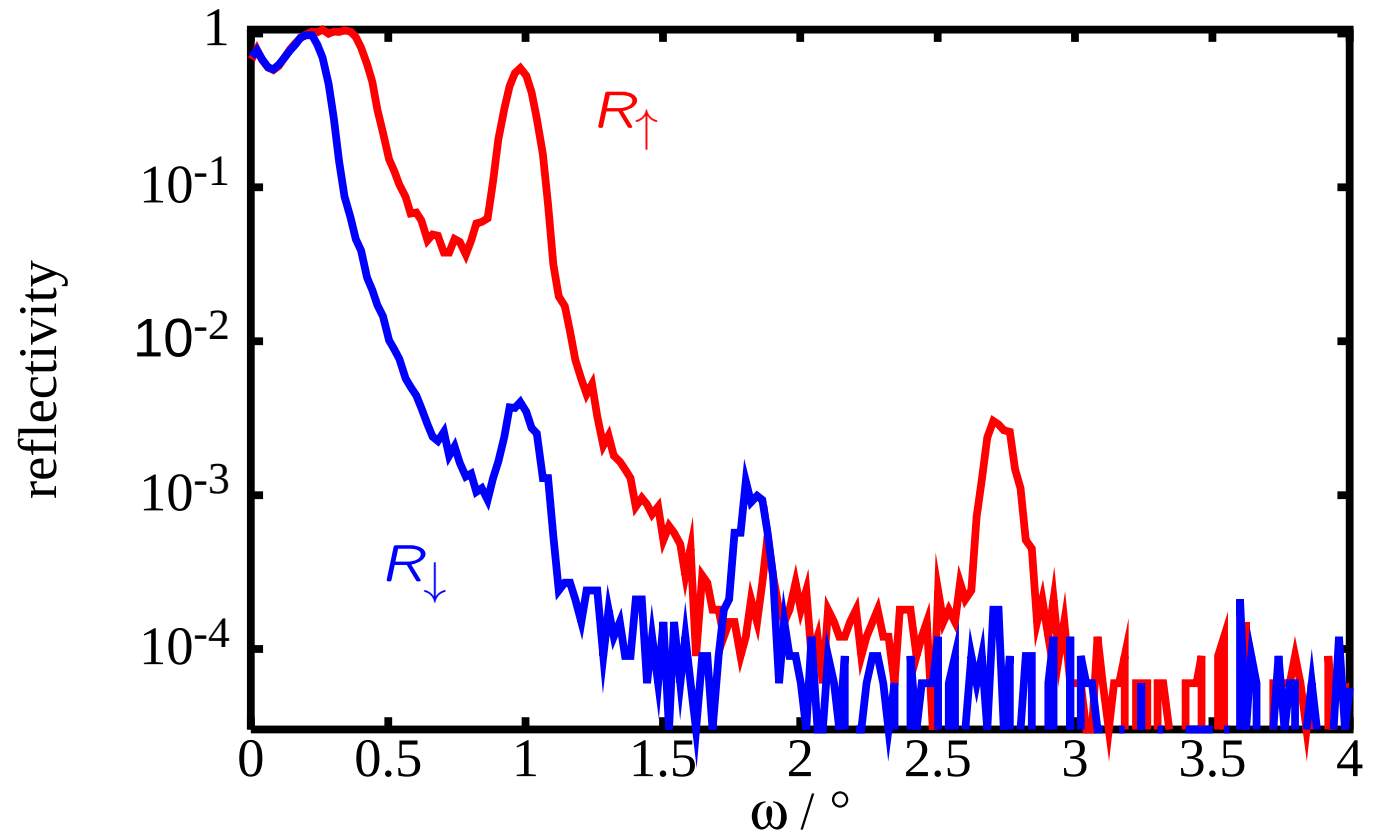


example:

Fe/Si multilayer on glass

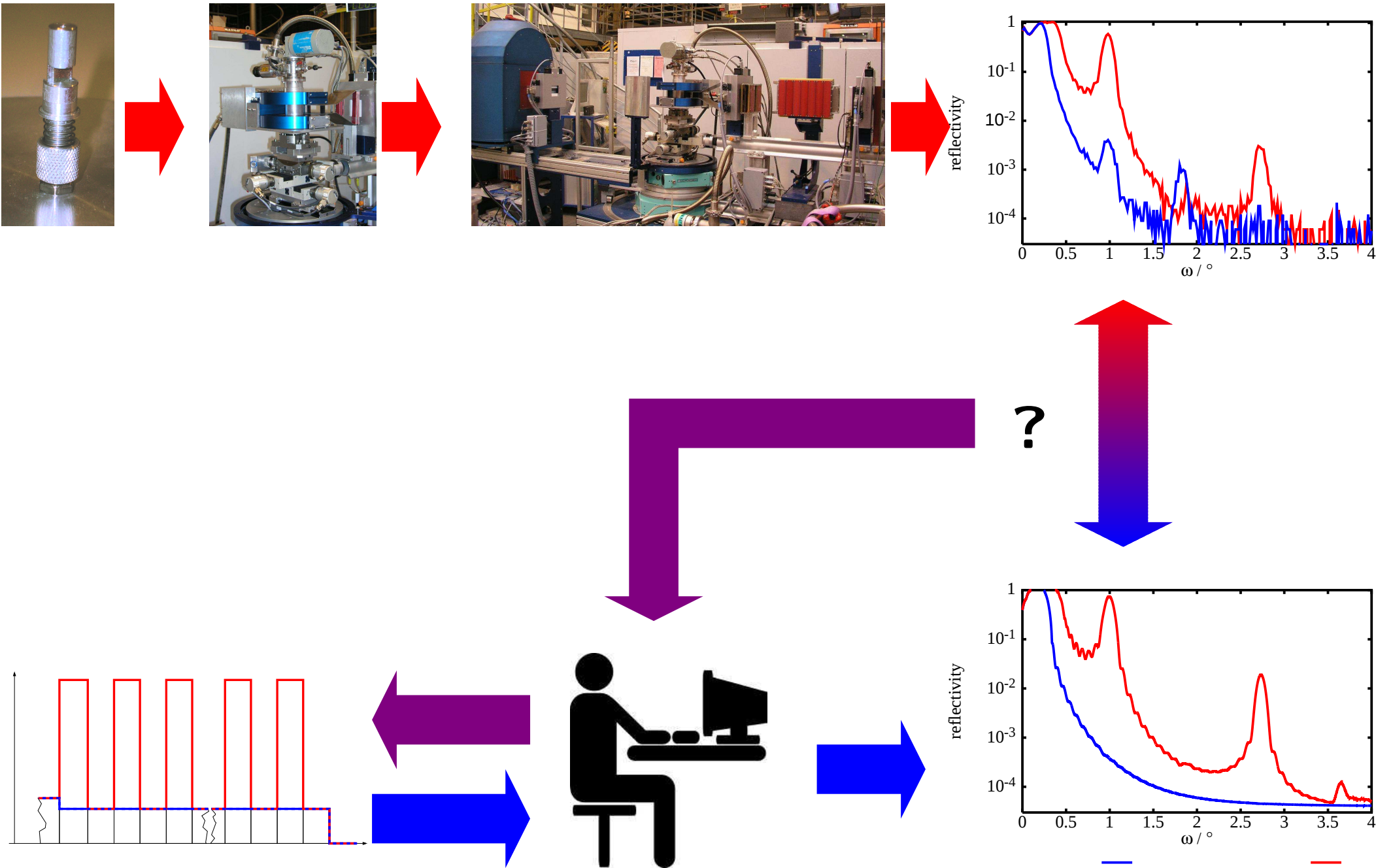
polarised neutrons

1h per spin state

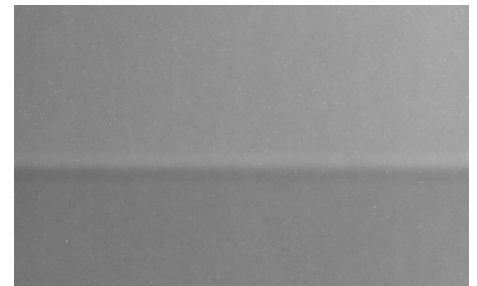
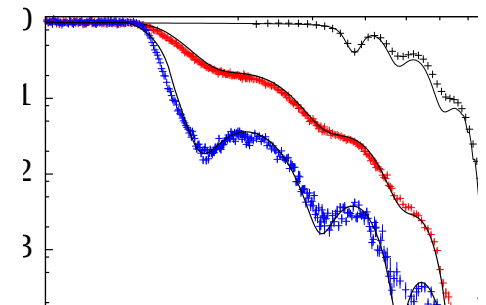
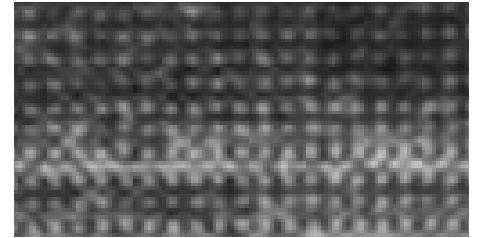


from the sample to $\rho(z)$

reflectometry 14



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flat surfaces partly reflect light

→ picture of the boot

some media also transmit light

→ ground below the water

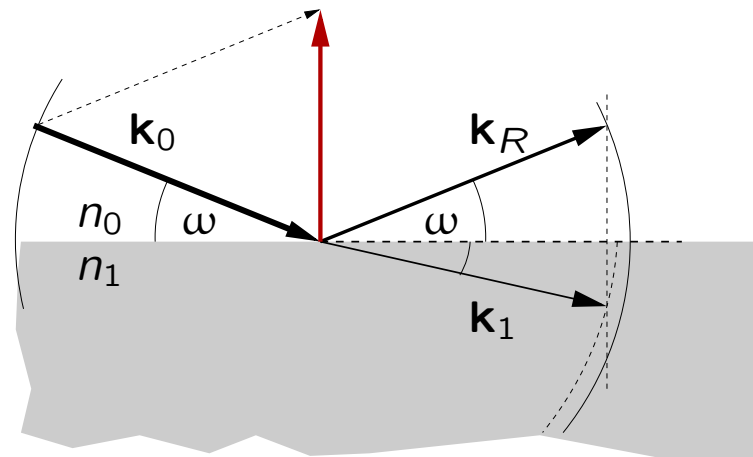
parallel interfaces

→ colourful soap bubbles



scientist's explanation:

- index of refraction,
- Fresnel reflectivity,
- transmittance,
- interference,
- bla bla bla ...



plane wave in a medium i :

$$\frac{\hbar^2}{2m} \frac{d^2}{dr^2} A e^{ik_i r} + (E - V_i) A e^{ik_i r} = 0$$

$$\frac{\hbar^2}{2m} (-k_i^2) e^{ik_i r} + (E - V_i) e^{ik_i r} = 0$$

$$\Rightarrow k_i^2 = (E - V_i) \frac{2m}{\hbar^2}$$

$$n_i^2 = \frac{k_i^2}{k_0^2}$$

by definition

$$= \frac{E - V_i}{E}$$

with $V_0 = 0$ (vacuum)

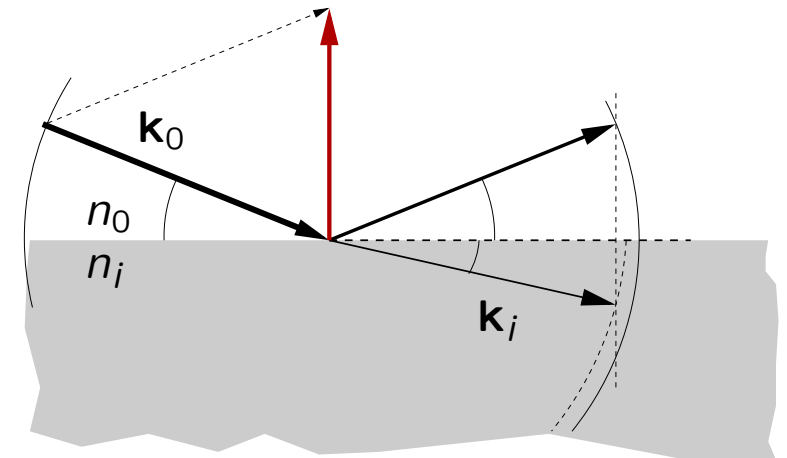
$$n_i = \sqrt{1 - V_i/E}$$

$$\approx 1 - V_i/2E$$

for $V_i \ll E$

$$:= 1 - \delta$$

$n_i - 1 \propto V_i \Rightarrow$ **what is V_i ?**



what is V_i for x-rays?

reflectometry 18

interaction γ / electron

(off-resonance)

$$\begin{aligned} V^e &= \frac{2\pi\hbar^2}{m_e} \frac{r_e}{\text{vol}} \sum_i Z_i \\ &= \frac{2\pi\hbar^2}{m_e} r_e \rho^e \end{aligned}$$

with

$$\begin{aligned} Z_i &= \text{electron number of atom } i \\ r_e &= \text{electron radius} \\ m_e &= \text{electron mass} \end{aligned}$$

$$\delta = \frac{\lambda^2}{2\pi} r_e \rho^e$$

with absorption: complex n

$$n = 1 - \delta - i\beta$$

at resonances:

$$\delta = \delta(\mathbf{B})$$

what is V_j for neutrons?

interaction neutron / nucleus j

with $\lambda \gg r_{\text{nucleus } j}$

interaction neutron magnetic moment μ
/ magnetic induction $\mathbf{B}$

$$\mu \uparrow\uparrow \mathbf{B} \Rightarrow V^m = +\mu B$$

$$\mu \uparrow\downarrow \mathbf{B} \Rightarrow V^m = -\mu B$$

$$\mu \perp \mathbf{B} \Rightarrow \text{spin-flip scattering}$$

reflectometry 19

$$V_j^{\text{Fermi}} = b_j \frac{2\pi \hbar^2}{m_n} \delta(\mathbf{r})$$

$$V^n = \frac{1}{\text{vol}} \int_j V_j^{\text{Fermi}} d\mathbf{r}$$

$$= \frac{2\pi \hbar^2}{m_n} \frac{1}{\text{vol}} \sum_j b_j$$

$$:= \frac{2\pi \hbar^2}{m_n} \rho^b$$

$$V^m = \mu \mathbf{B}_\perp$$

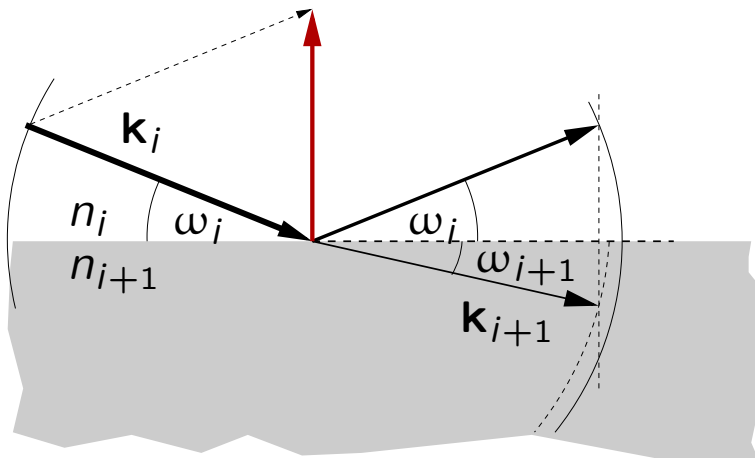
$$:= \frac{2\pi \hbar^2}{m_n} \rho^m$$

$$m_n = \text{neutron mass}$$

what is the reflected intensity?

assumptions:

- one interface, only
- ideally flat and sharp
- homogeneous in x and y
 $\Rightarrow$ only normal (z) components are relevant



continuity conditions for a plane wave impinging on the interface $i, i + 1$:

$$\Psi_{z,i} = \Psi_{z,i+1}$$

$$\frac{d}{dz}\Psi_{z,i} = \frac{d}{dz}\Psi_{z,i+1}$$

with

$$\Psi_{z,j} = A_j^{\uparrow} e^{ik_{z,j}z} + A_j^{\downarrow} e^{-ik_{z,j}z}$$

$$\begin{aligned} k_{z,j} &= k_j \sin \omega_j \\ &= n_j k_0 \sin \omega_j \end{aligned}$$

reflectance

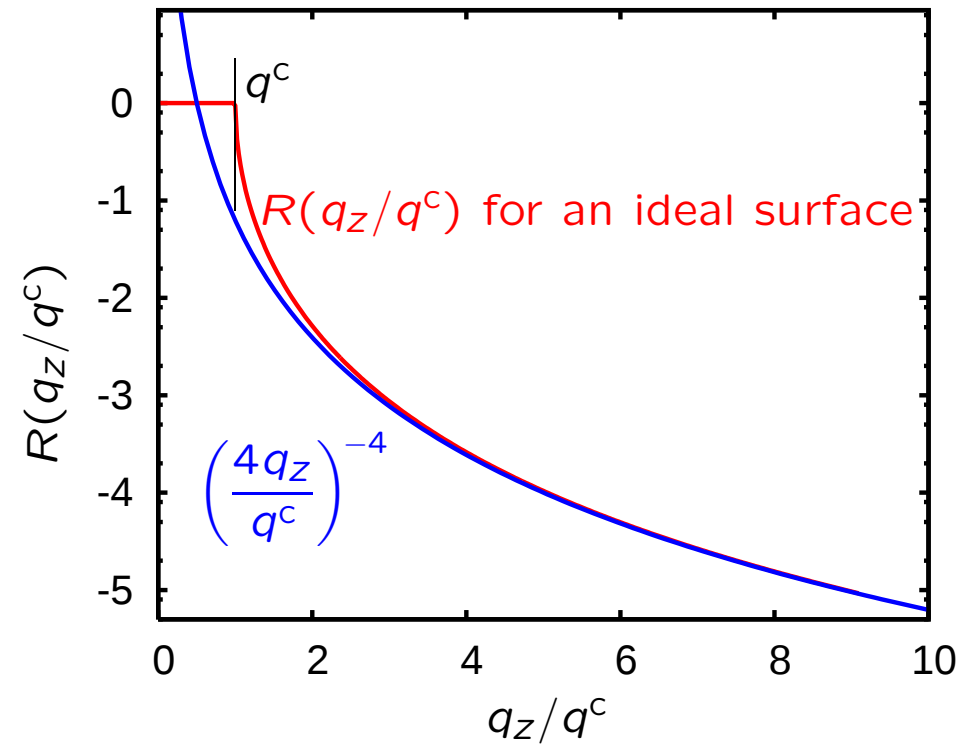
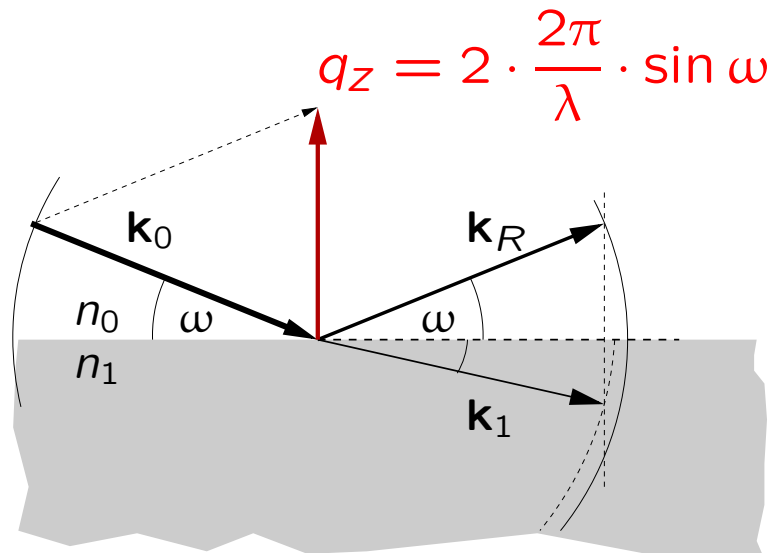
$$\begin{aligned} r_{i,i+1} &= \frac{A_i^{\uparrow}}{A_i^{\downarrow}} \\ &\vdots \\ &= \frac{n_i \sin \omega_i - n_{i+1} \sin \omega_{i+1}}{n_i \sin \omega_i + n_{i+1} \sin \omega_{i+1}} \end{aligned}$$

reflectance for $\omega_{i+1} > 0$

$$r_{i,i+1} = \frac{n_i \sin \omega_i - n_{i+1} \sin \omega_{i+1}}{n_i \sin \omega_i + n_{i+1} \sin \omega_{i+1}}$$

transmittance for $\omega_{i+1} > 0$

$$t_{i,i+1} = \frac{2 n_i \sin \omega_i}{n_i \sin \omega_i + n_{i+1} \sin \omega_{i+1}}$$



air/solid interface for $q_z > q^c$

$$r_{0,1} = \frac{1 - \sqrt{1 - (q^c/q_z)^2}}{1 + \sqrt{1 - (q^c/q_z)^2}}$$

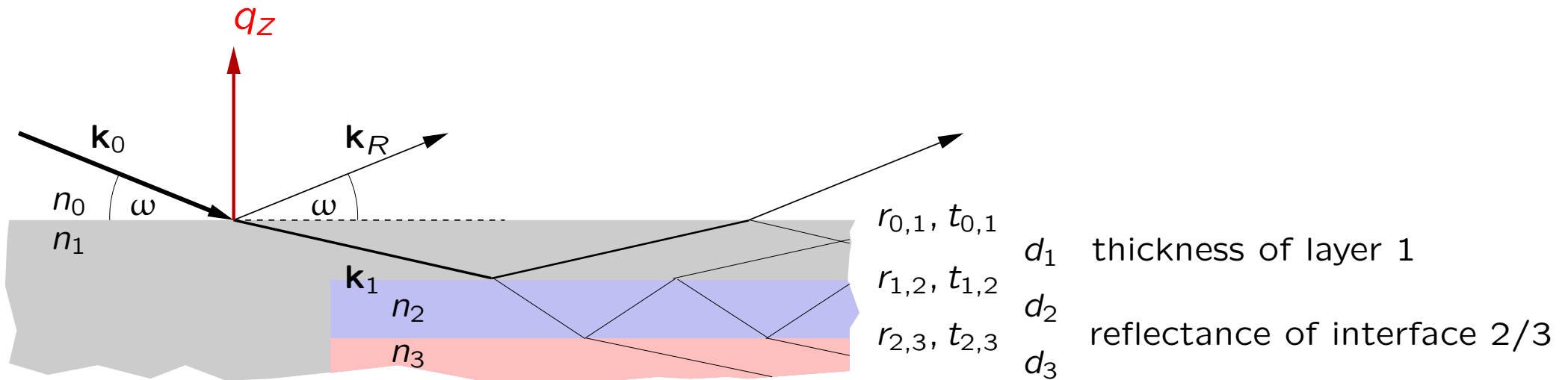
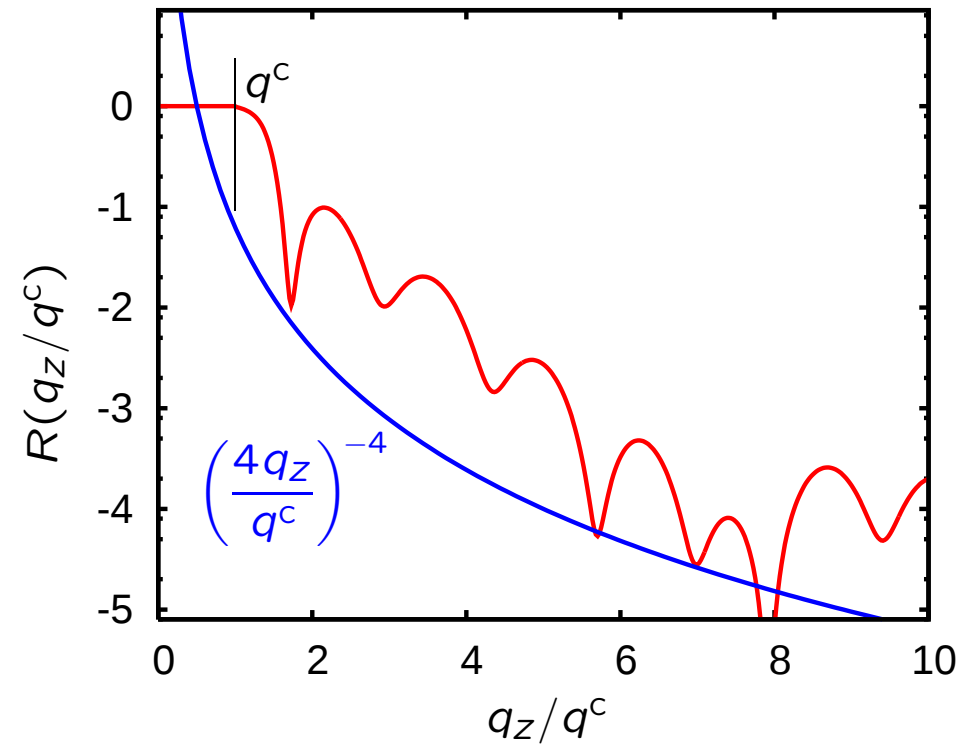
$$R(q_z) = |r_{0,1}(q_z)|^2$$

several parallel interfaces:

interference of all waves

$$R(q_z) = |r(q_z)|^2$$

what is $r(q_z)$ of a multilayer?



$$\Psi_0(0) = \begin{pmatrix} A_0^\uparrow \\ A_0^\downarrow \end{pmatrix} \quad \text{free choice of phase}$$

$$= \begin{pmatrix} 1/t_{0,1} & r_{0,1}/t_{0,1} \\ r_{0,1}/t_{0,1} & 1/t_{0,1} \end{pmatrix} \begin{pmatrix} A_1^\uparrow \\ A_1^\downarrow \end{pmatrix} \quad \text{continuity condition}$$

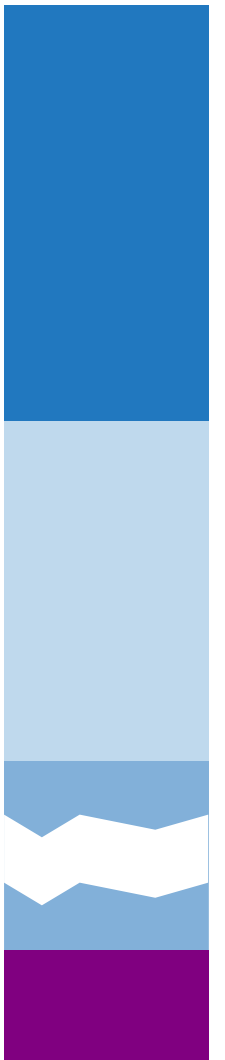
$$= \mathbf{I}_{0,1} \begin{pmatrix} e^{ik_{z,1}d_1} & 0 \\ 0 & e^{-ik_{z,1}d_1} \end{pmatrix} \begin{pmatrix} A_1^\uparrow e^{-ik_{z,1}d_1} \\ A_1^\downarrow e^{ik_{z,1}d_1} \end{pmatrix} \quad \text{phase factor}$$

$$= \mathbf{I}_{0,1} \mathbf{T}_1 \begin{pmatrix} 1/t_{1,2} & r_{1,2}/t_{1,2} \\ r_{1,2}/t_{1,2} & 1/t_{1,2} \end{pmatrix} \begin{pmatrix} A_2^\uparrow e^{-ik_{z,1}d_1} \\ A_2^\downarrow e^{ik_{z,1}d_1} \end{pmatrix}$$

$$= \mathbf{I}_{0,1} \mathbf{T}_1 \mathbf{I}_{1,2} \begin{pmatrix} e^{ik_{z,2}d_2} & 0 \\ 0 & e^{-ik_{z,2}d_2} \end{pmatrix} \begin{pmatrix} A_2^\uparrow e^{-ik_{z,2}(d_1+d_2)} \\ A_2^\downarrow e^{ik_{z,2}(d_1+d_2)} \end{pmatrix}$$

$$\vdots$$

$$:= \mathbf{M} \begin{pmatrix} A_{\text{substr}}^\uparrow e^{-ik_{z,\text{substr}} \sum_i d_i} \\ A_{\text{substr}}^\downarrow e^{ik_{z,\text{substr}} \sum_i d_i} \end{pmatrix}$$



$$\psi_0(0) = \begin{pmatrix} A_0^\uparrow \\ A_0^\downarrow \end{pmatrix}$$

$$= \mathbf{M} \begin{pmatrix} 0 \\ A_{\text{substr}}^\downarrow e^{ik_{z,\text{substr}} \sum_i d_i} \end{pmatrix}$$

$$r(q_z) = A_0^\uparrow / A_0^\downarrow$$

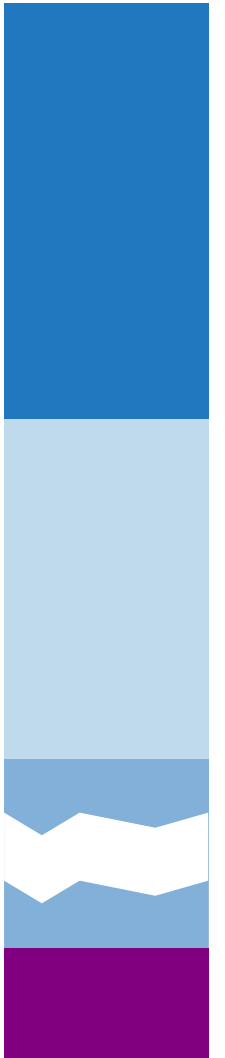
$$= \frac{M_{12} A_{\text{substr}}^\downarrow e^{ik_{z,\text{substr}} \sum_i d_i}}{M_{22} A_{\text{substr}}^\downarrow e^{ik_{z,\text{substr}} \sum_i d_i}}$$

$$= \frac{M_{12}(q_z)}{M_{22}(q_z)}$$

calculation of $M_{12}(q_z)$ and $M_{22}(q_z)$ is trivial ...

... if all n_i and d_i are known!

there is no
upcoming
wave



$$R(q_z) = |r(q_z)|^2$$

⇒ all phase information is lost

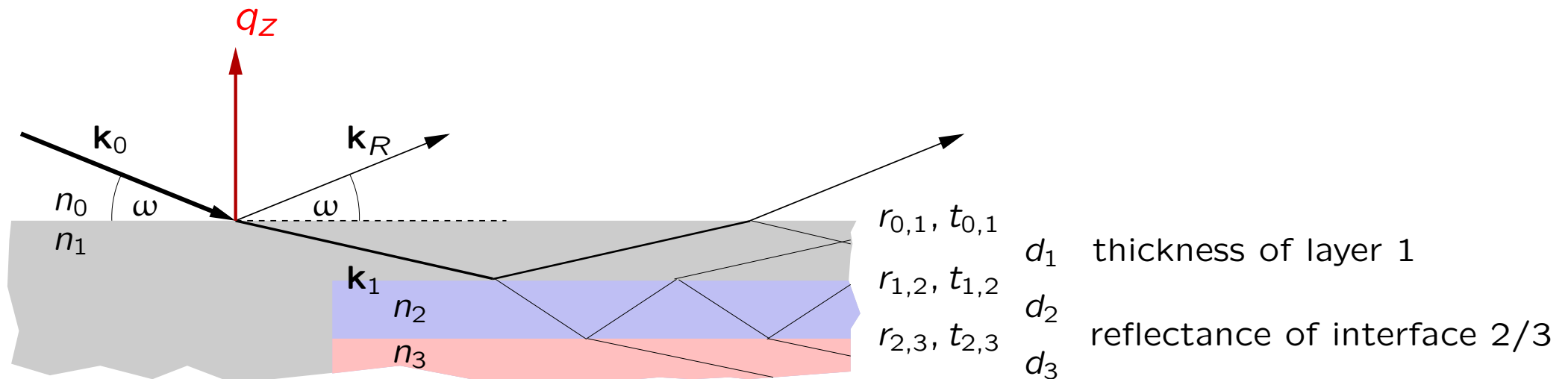
⇒ one way road:

⇒ calculation of $R(q_z)$ using a model
and
comparison to measured curve(s)

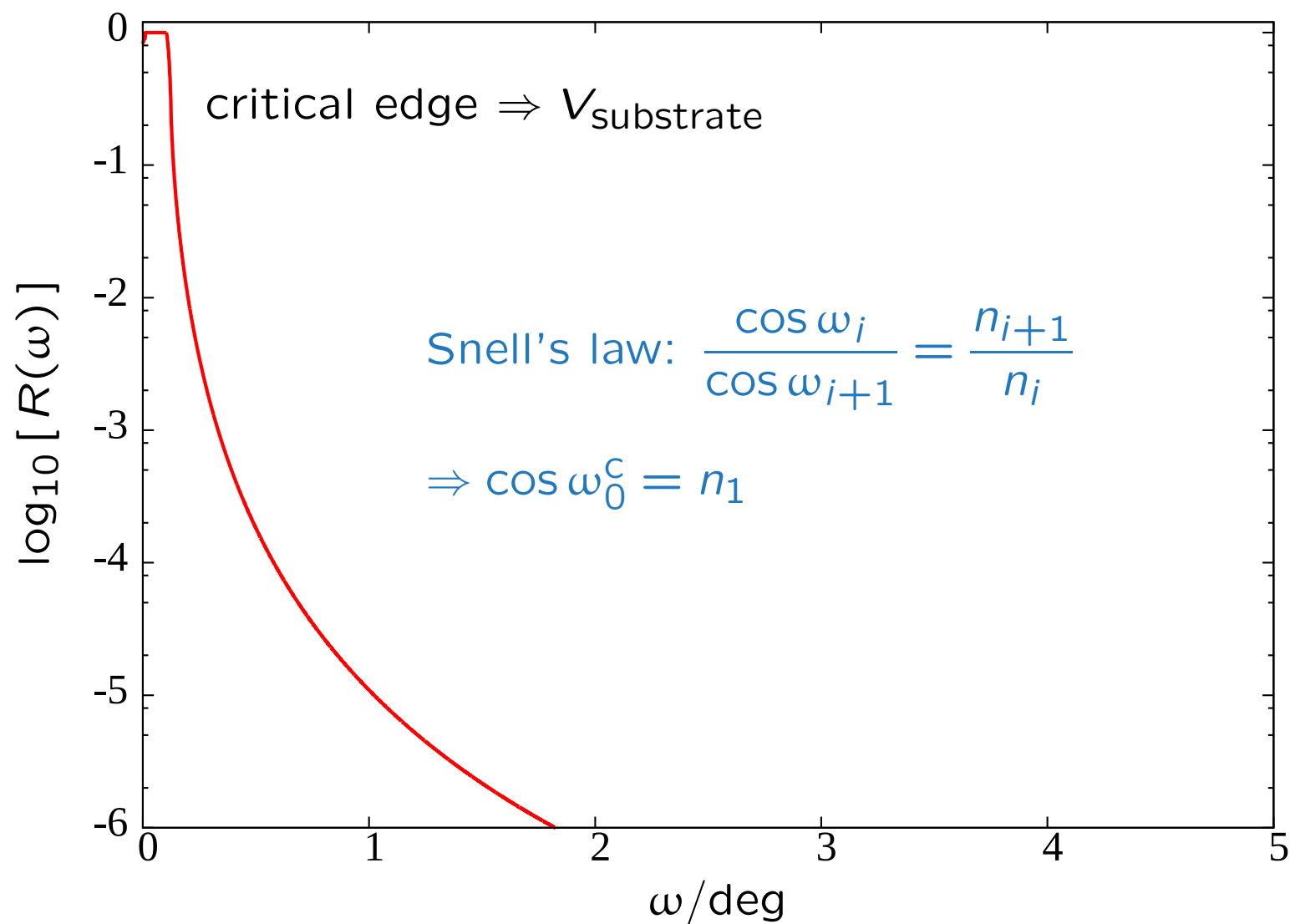
real effects

to be taken into account:

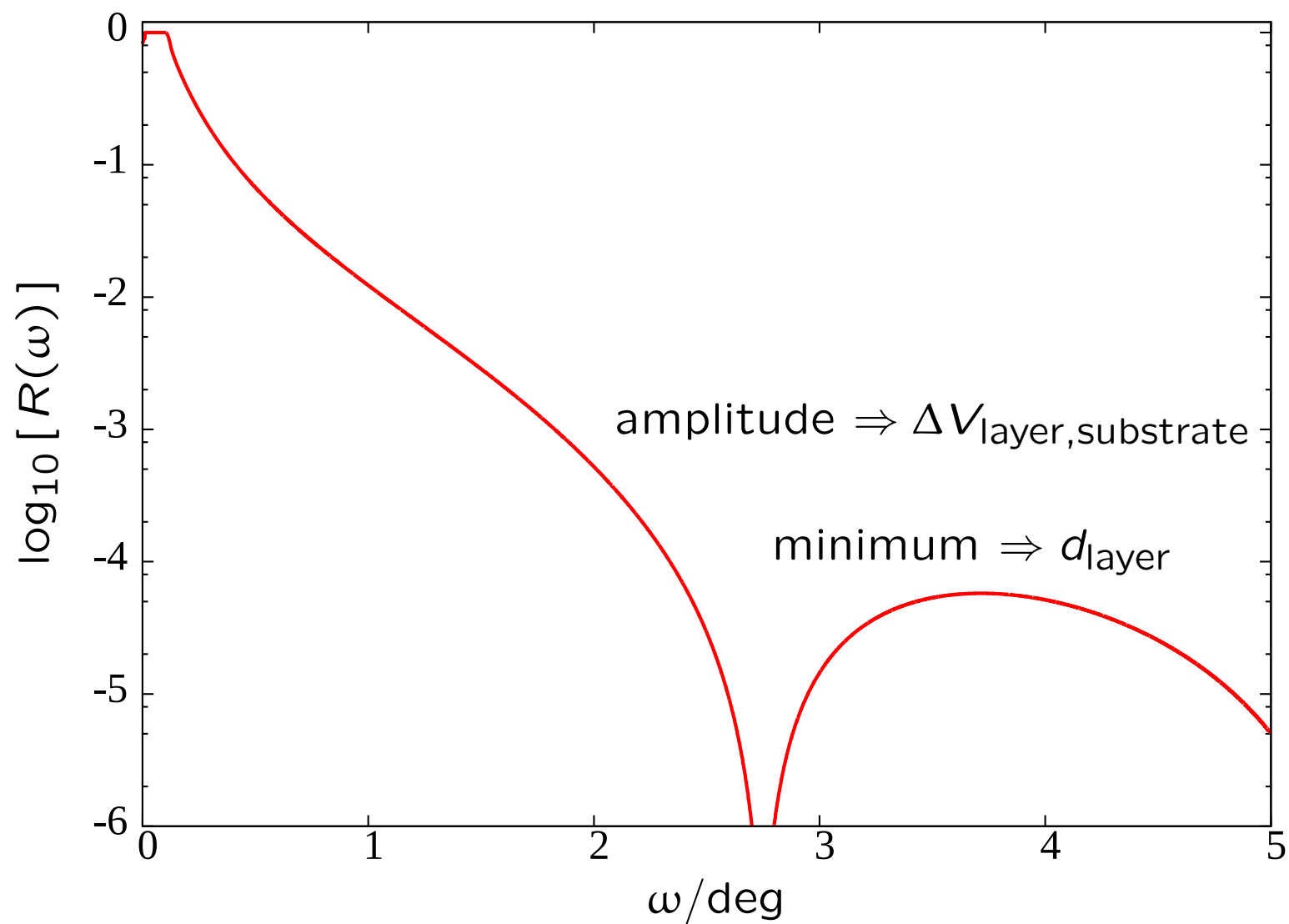
- non-sharp interfaces
- inhomogeneous layers
- illumination of the sample
- resolution of the set-up
 $\Delta\omega, \Delta\lambda$



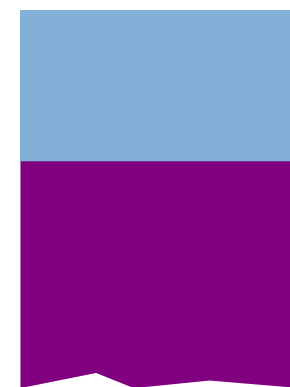
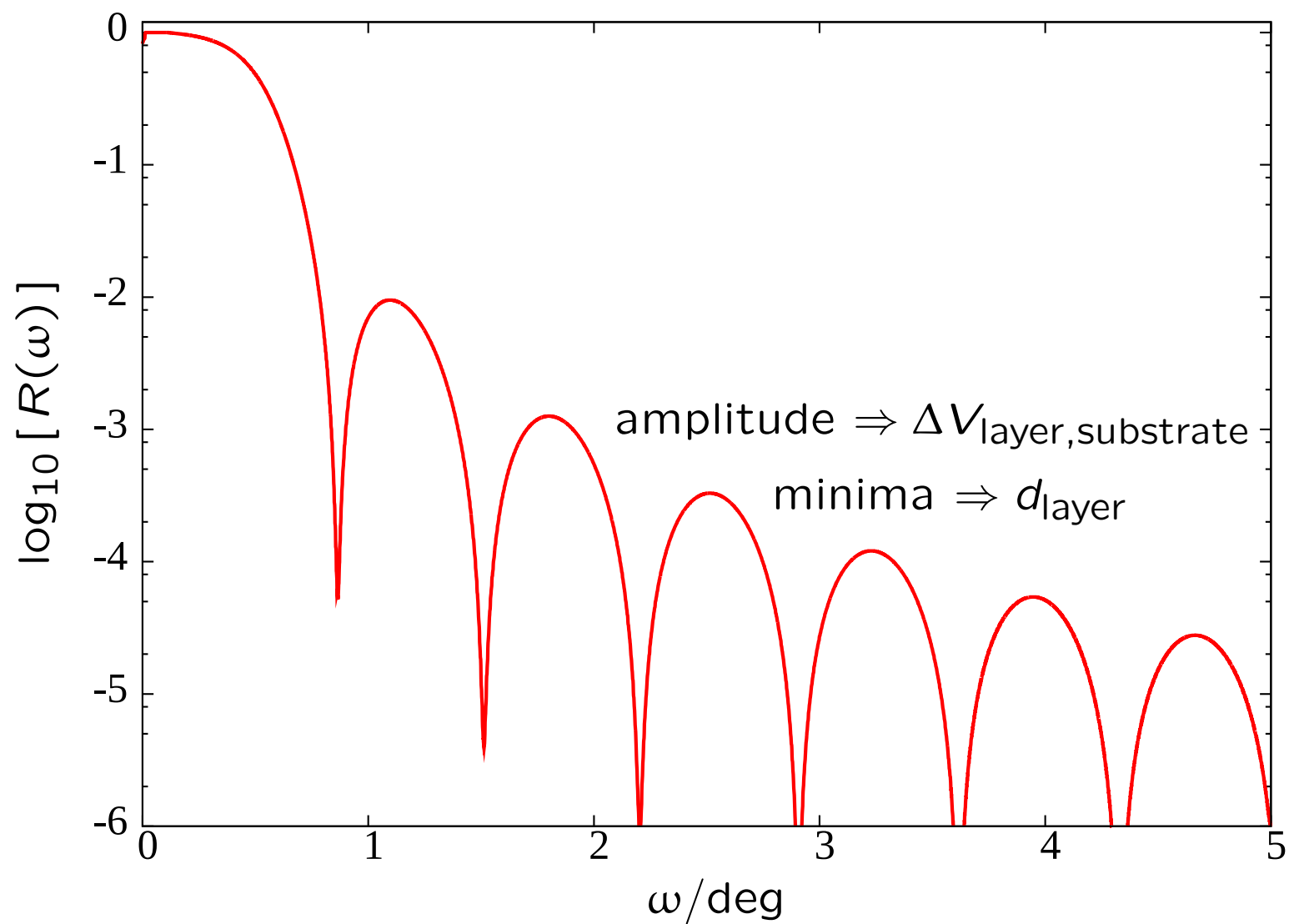
... of a surface



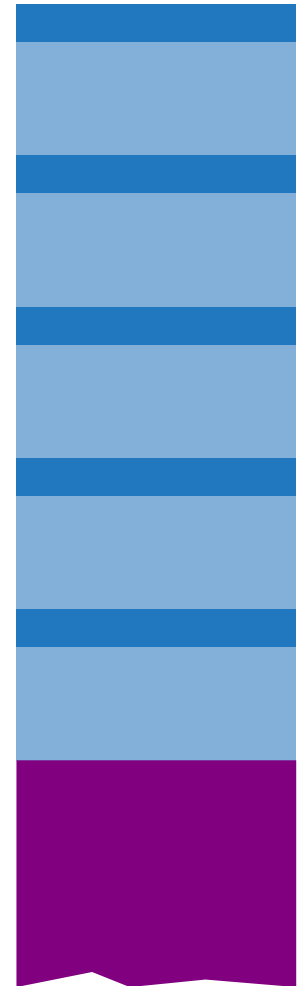
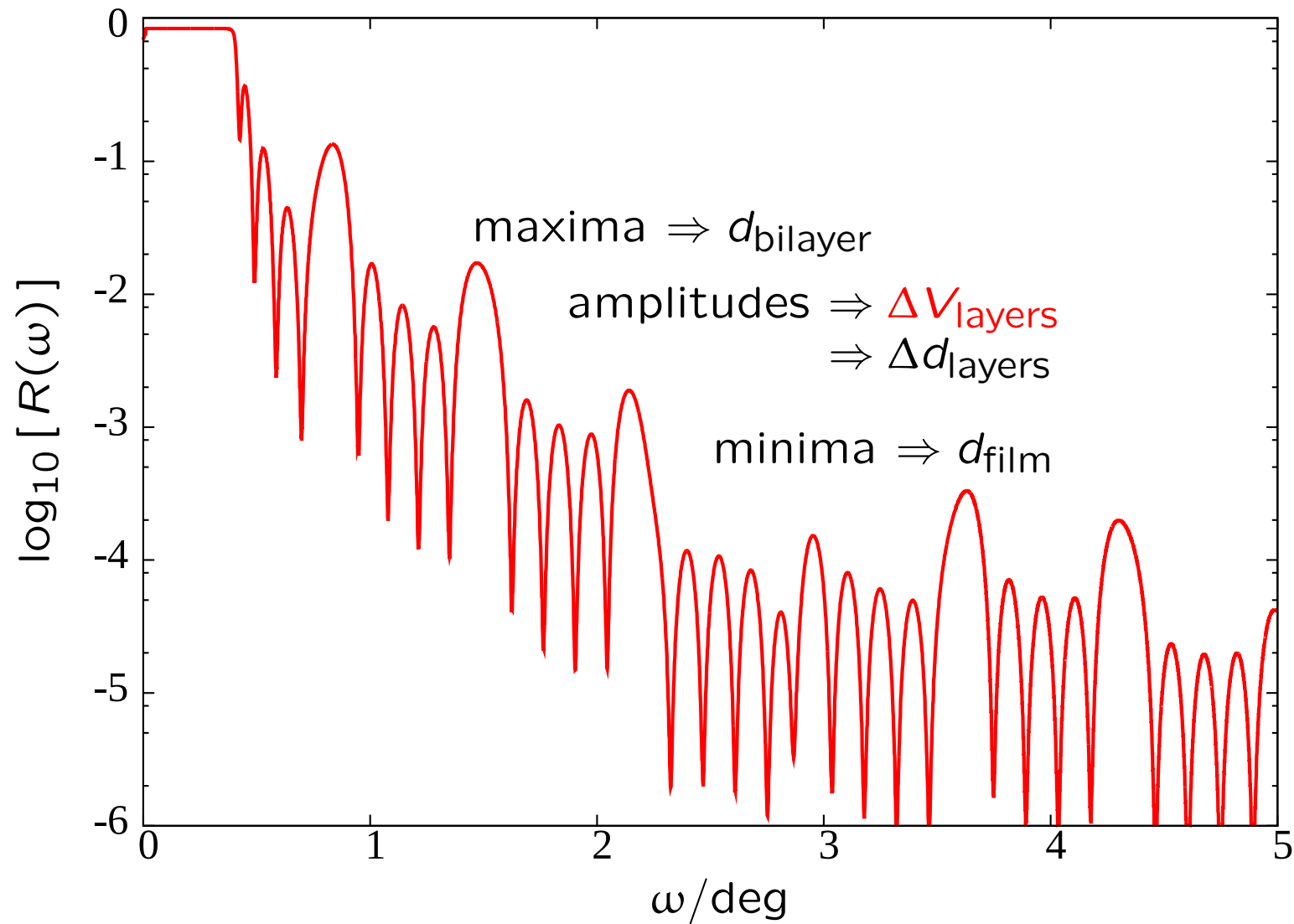
... of a thin layer



... of a thick layer



... of a periodic multilayer



$$\delta = 1 - n = \frac{\lambda^2}{2\pi} (\rho^b + \rho^m) \text{ for neutrons}$$
$$= \frac{\lambda^2}{2\pi} r_e \rho^e \text{ for x-rays}$$

$$\text{Ni: } \rho^b = 9.4 \cdot 10^{-6} \text{ \AA}^{-2}$$

$$\Rightarrow \delta^{\text{nuc}} = 3.75 \cdot 10^{-5}, \lambda = 5 \text{ \AA}$$

$$\Rightarrow \omega^c \approx 0.5^\circ$$

$$\delta \ll 1$$

small angles of incidence!

$$\text{Fe: } \rho^m \approx 6 \cdot 10^{-6} \text{ \AA}^{-2}$$

$$\Rightarrow \delta^m \approx 2.4 \cdot 10^{-5}, \lambda = 5 \text{ \AA}$$

$$\delta^m \sim \delta^b$$

$$\text{Al: } r_e \rho^e = 2.2 \cdot 10^{-5} \text{ \AA}^{-2}$$

$$\Rightarrow \delta^e = 8.7 \cdot 10^{-5}, \lambda = 5 \text{ \AA}$$

$$\delta^e \sim \delta^b$$

probed depth 100 nm $\rightarrow$ 1 μ m

(less for strong absorbers)

depth resolution 0.2 nm $\rightarrow$ 400 nm

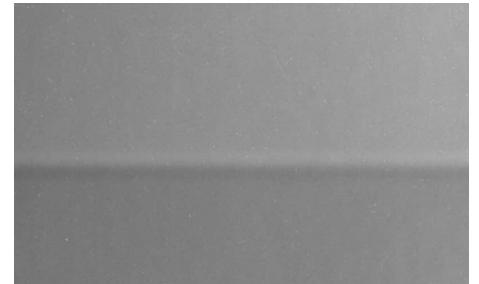
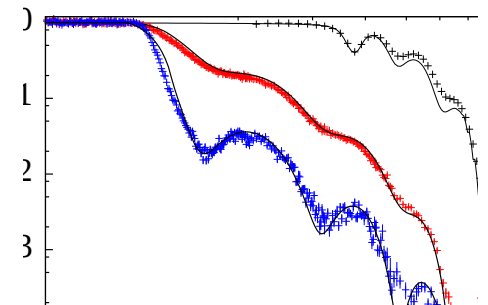
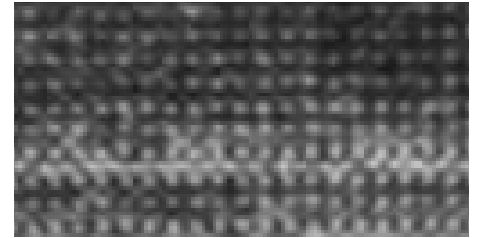
strongly model dependent

t and δ might be strongly correlated

lateral coherence 1 μ m $\rightarrow$ 100 μ m

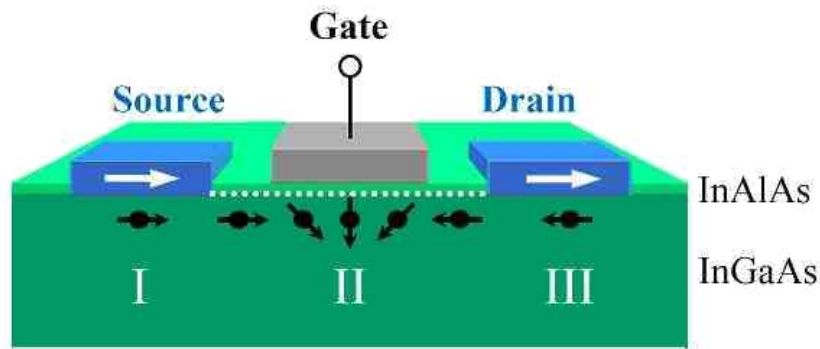
averaging laterally over all
microstructures

- heterostructures
 - magnetic layers
 - membrane systems
- reflectometry
 - (few formulae)
- ... derivation
 - (lots of formulae)
- experimental examples
 - Fe/Si
 - FeSi/GaAs interfaces
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- relevance for imaging
 - YES, there is some!



use not only the electron charge to carry information but also its spin

e.g. transistor based on spin / FM alignment:



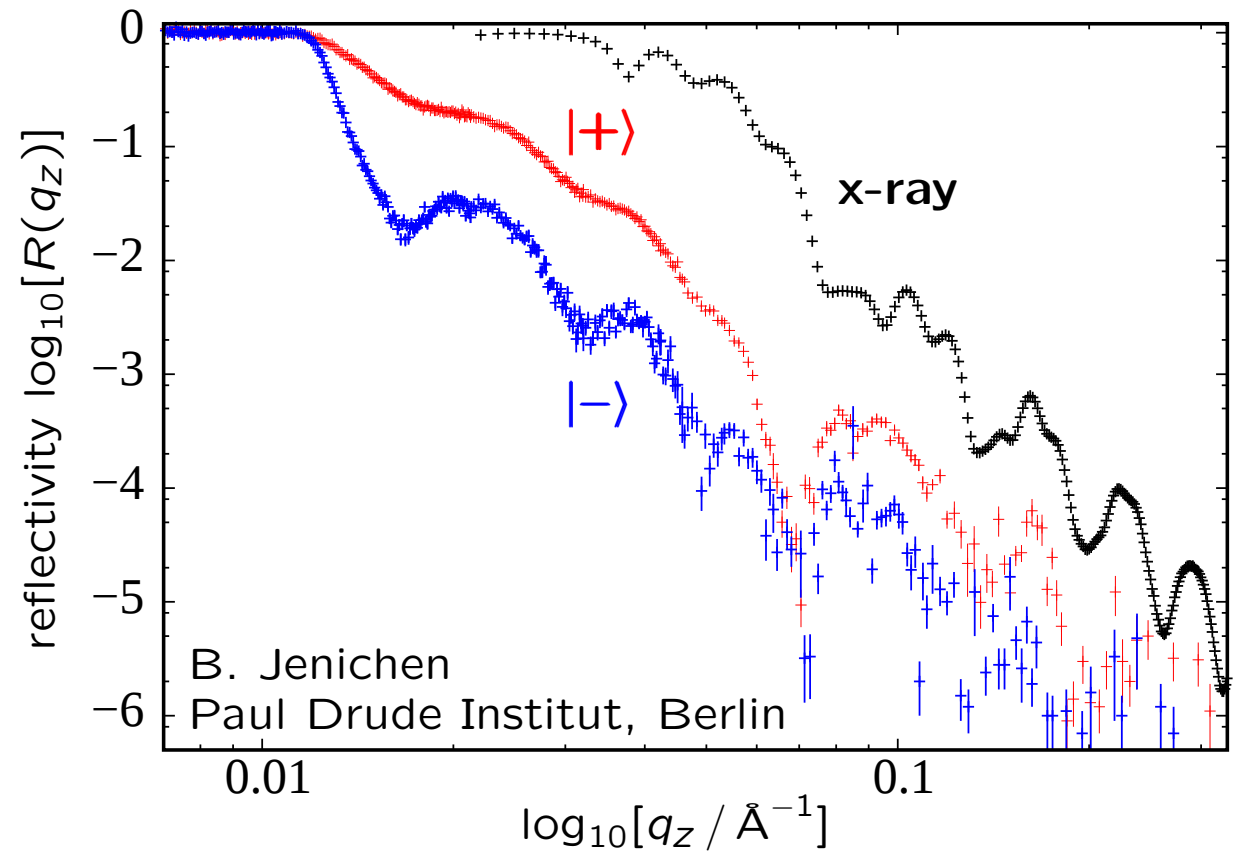
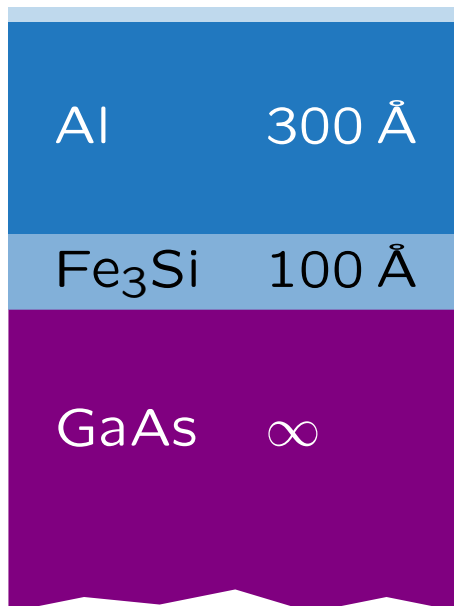
spin-polarised currents exist in *half-metals* (e.g. Fe_3Si)

but

polarised spin injection into a semiconductor (e.g. GaAs) is inefficient

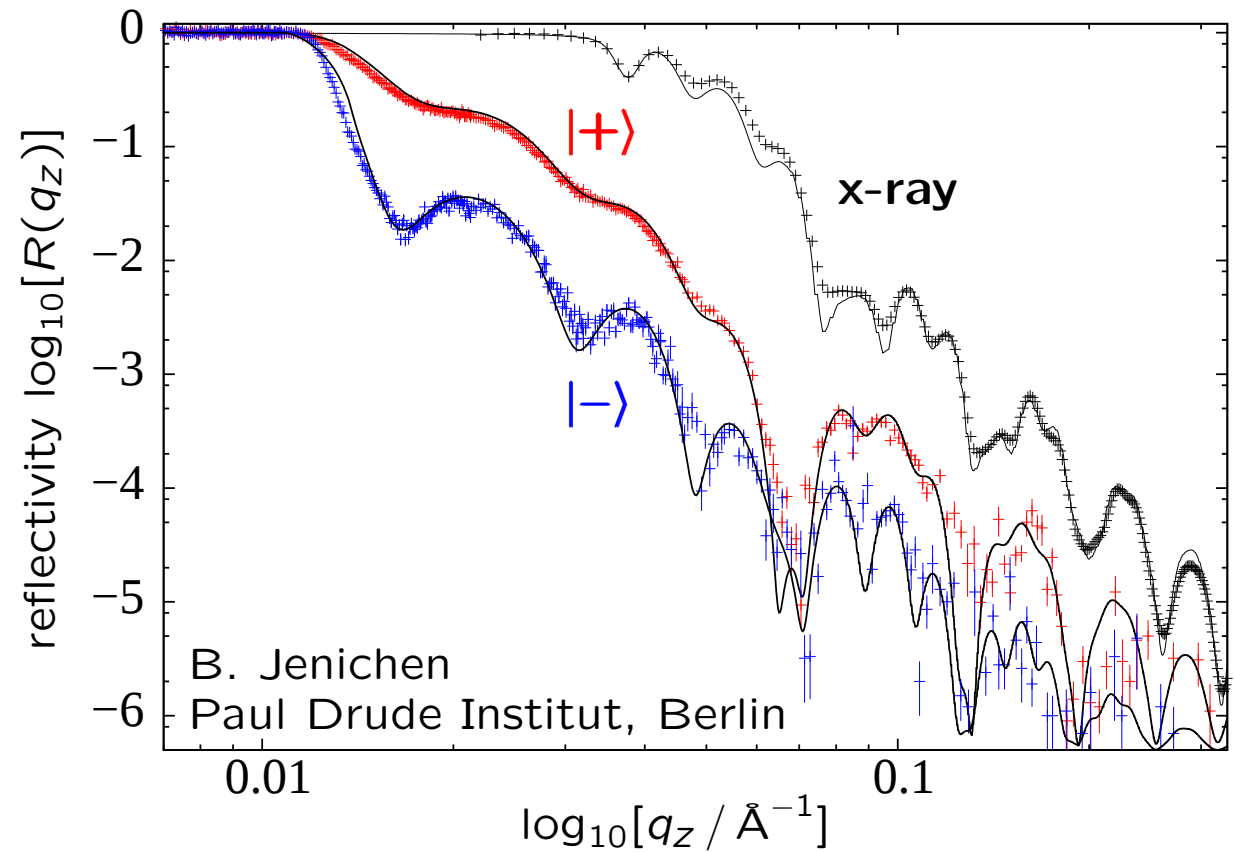
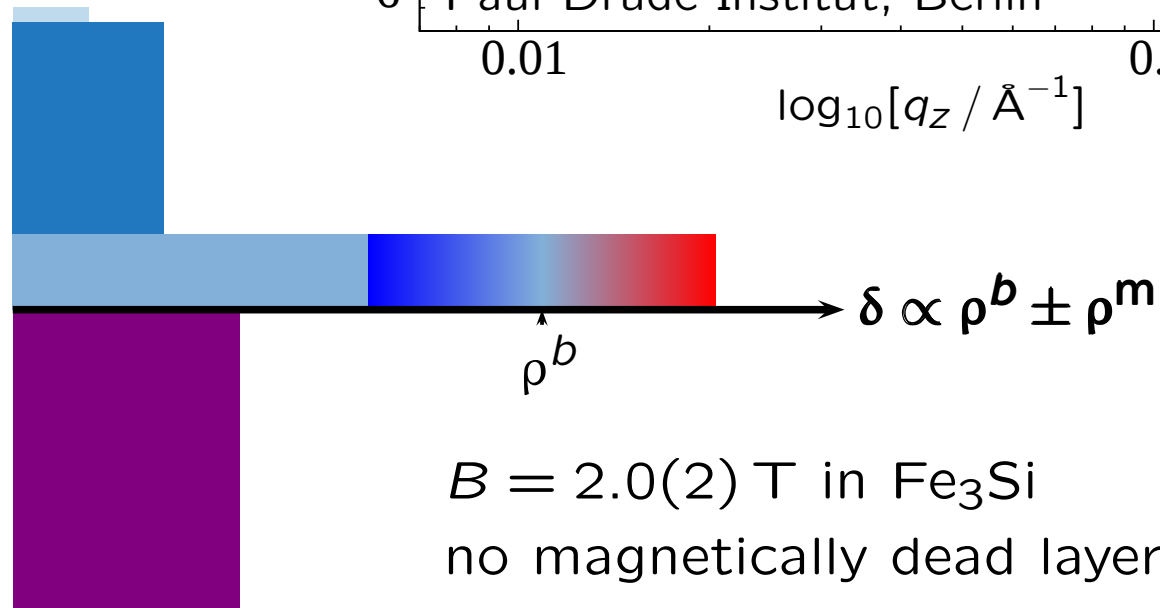
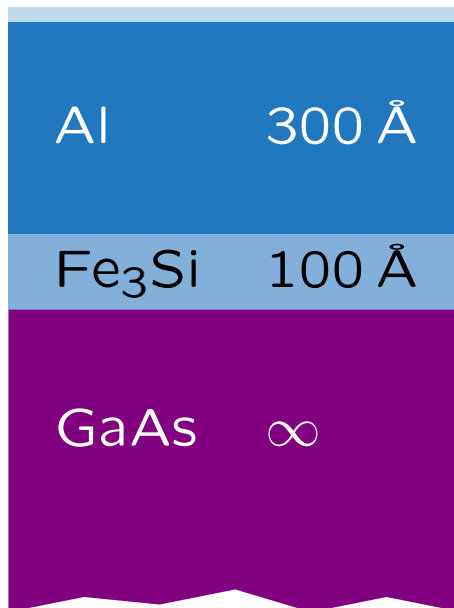
⇒ what happens at the interface?

Fe₃Si film on GaAs
search for a magnetically
dead layer



sample size: $5 \times 5 \text{ mm}^2$
measurement time: 24 h neutron
1 h x-ray

Fe₃Si film on GaAs
search for a magnetically
dead layer

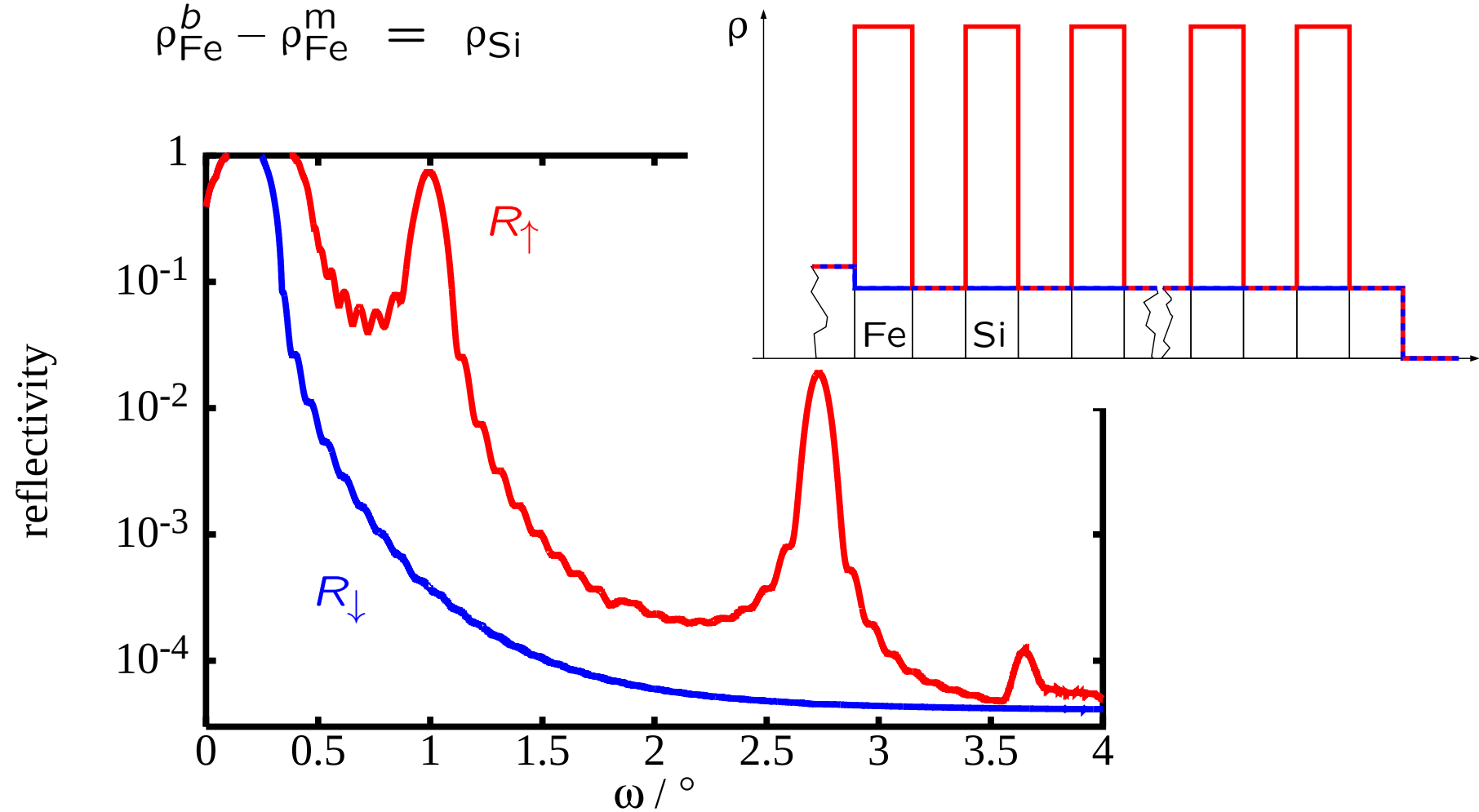


Fe/Si multilayer

ideal case:

$$\rho_{\text{Fe}}^b + \rho_{\text{Fe}}^m \gg \rho_{\text{Si}}$$

$$\rho_{\text{Fe}}^b - \rho_{\text{Fe}}^m = \rho_{\text{Si}}$$

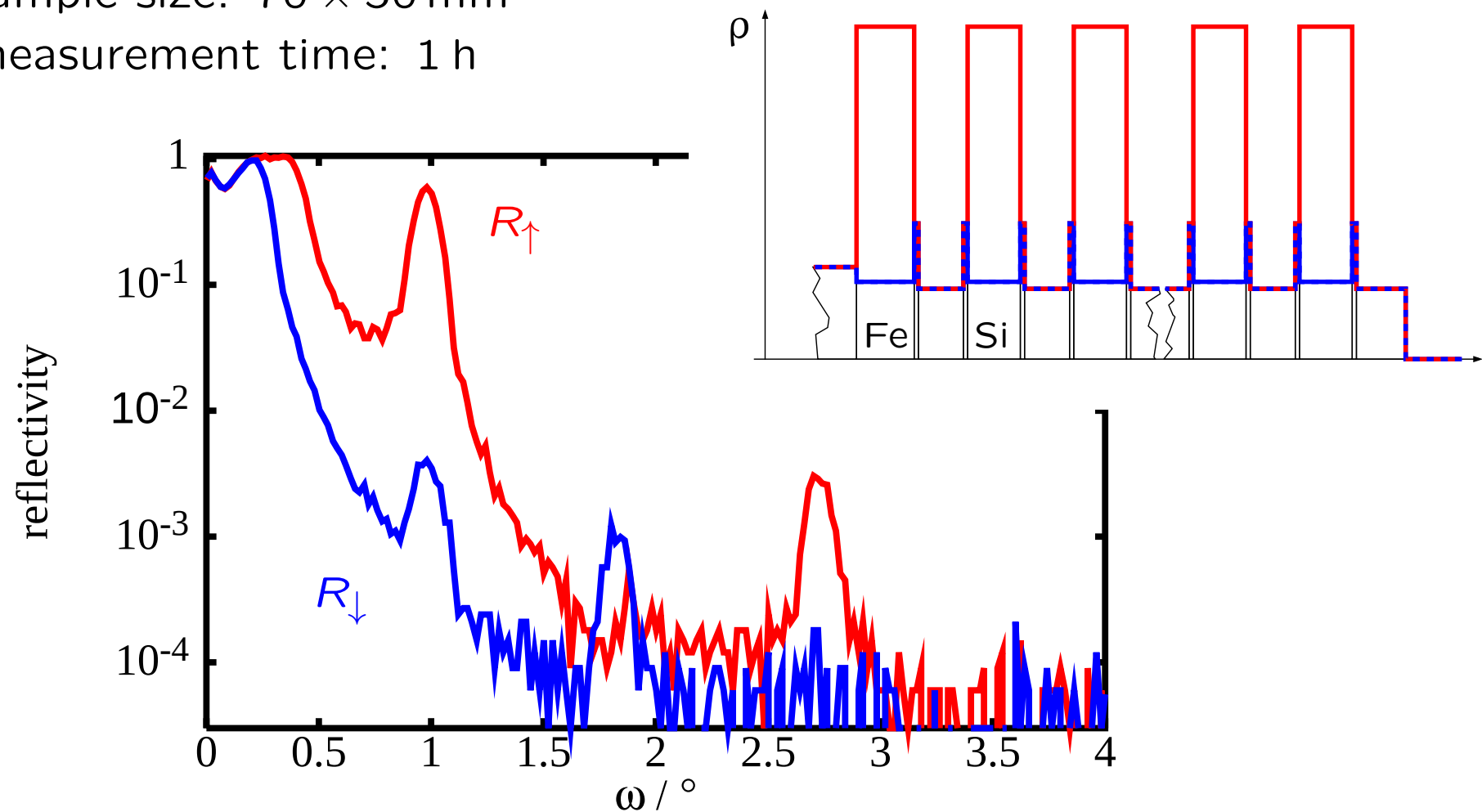


Fe/Si multilayer

reality: interdiffusion leads to 5 Å thin magnetically dead Fe : Si layers

sample size: $70 \times 50 \text{ mm}^2$

measurement time: 1 h

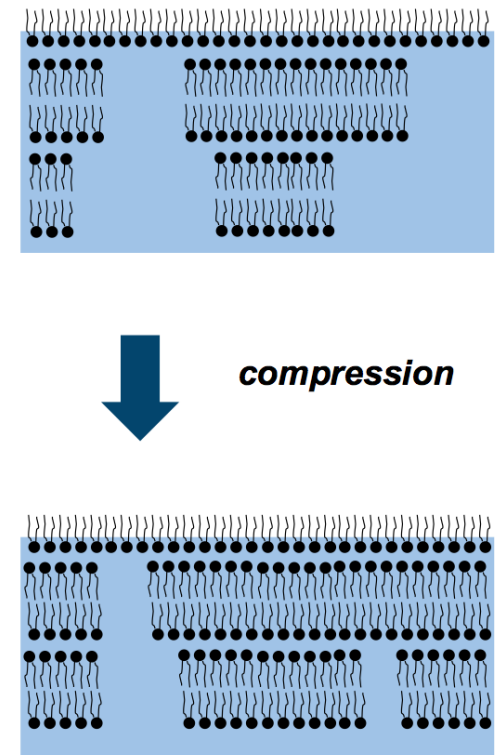
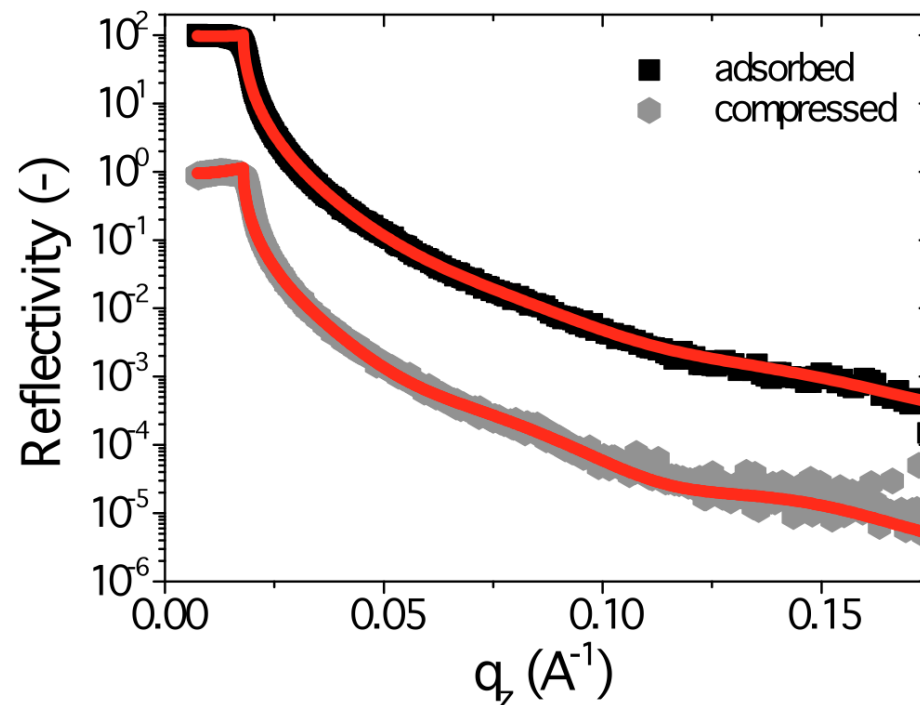


compression of self-organising polyglycerol-ester films

H₂O substituted by D₂O

⇒ strong contrast between solvent and film (essentially [CH₂]_n)

⇒ *high* critical edge



constant film thickness

laterally more homogeneous

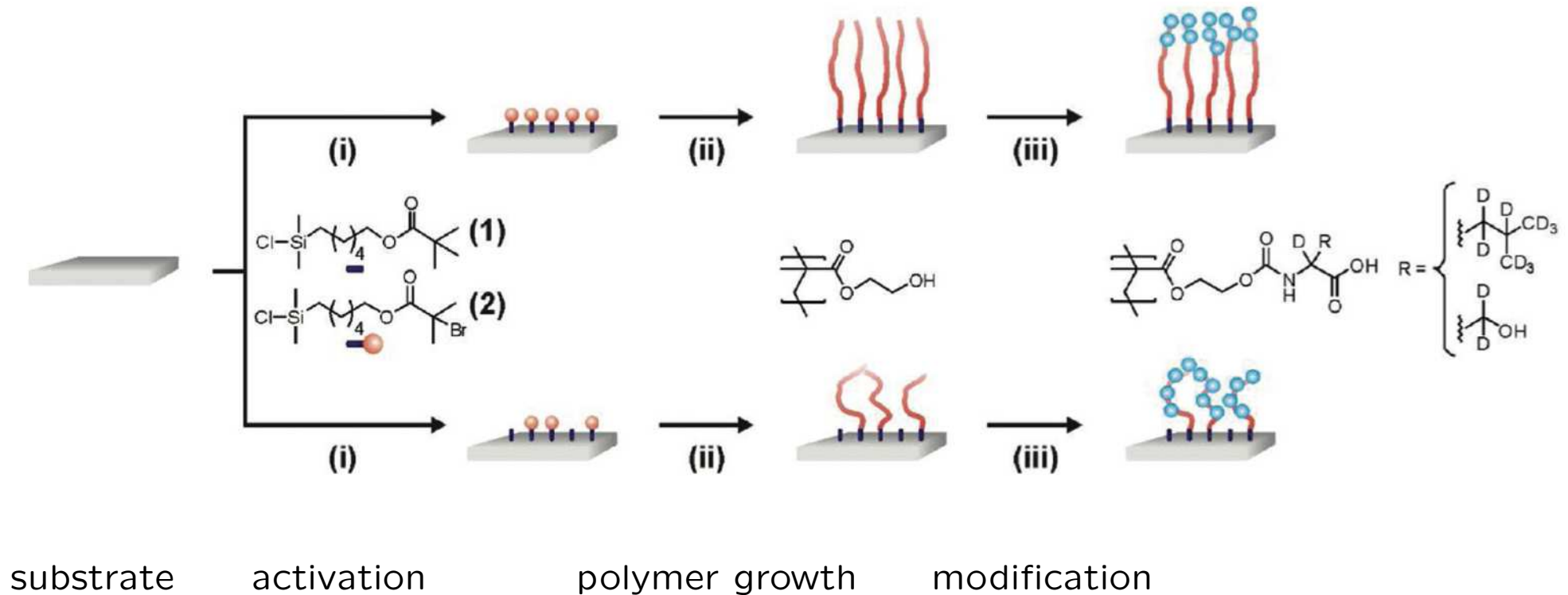
⇒ less *roughness*

⇒ lower damping of $R(q_z)$

polymer brushes

- applications:
- anti-fouling color
 - coating within ball bearings
 - **matrix for chemical sensors**

where are the functional groups located?



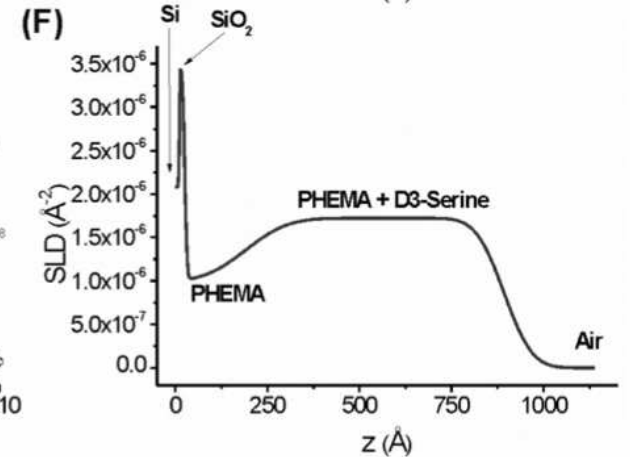
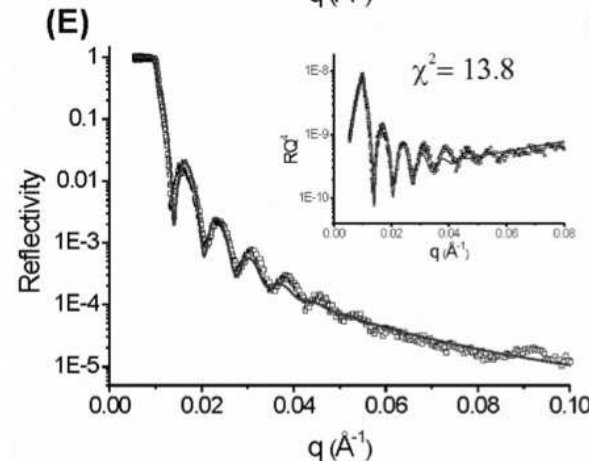
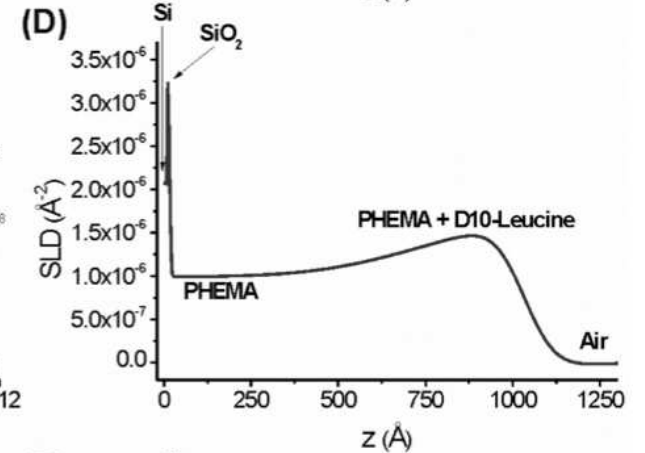
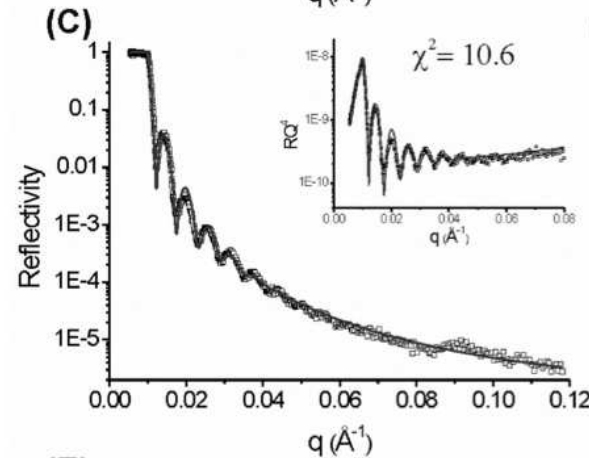
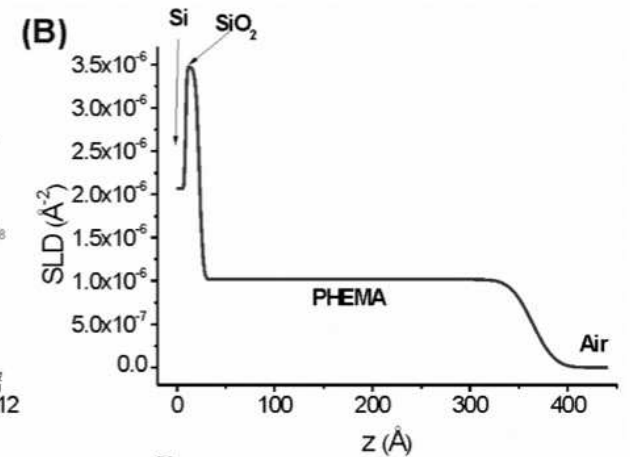
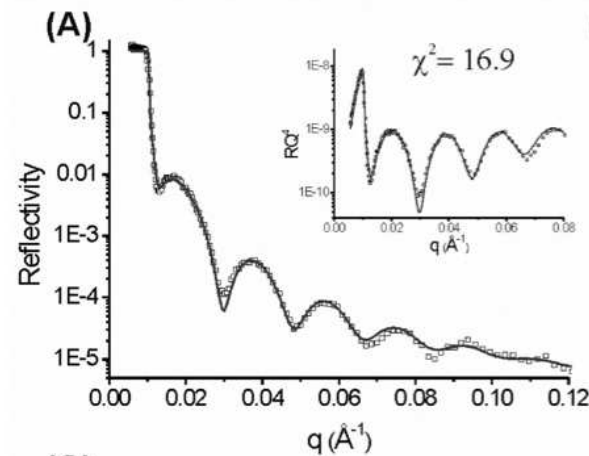
polymer brushes

location of functional groups

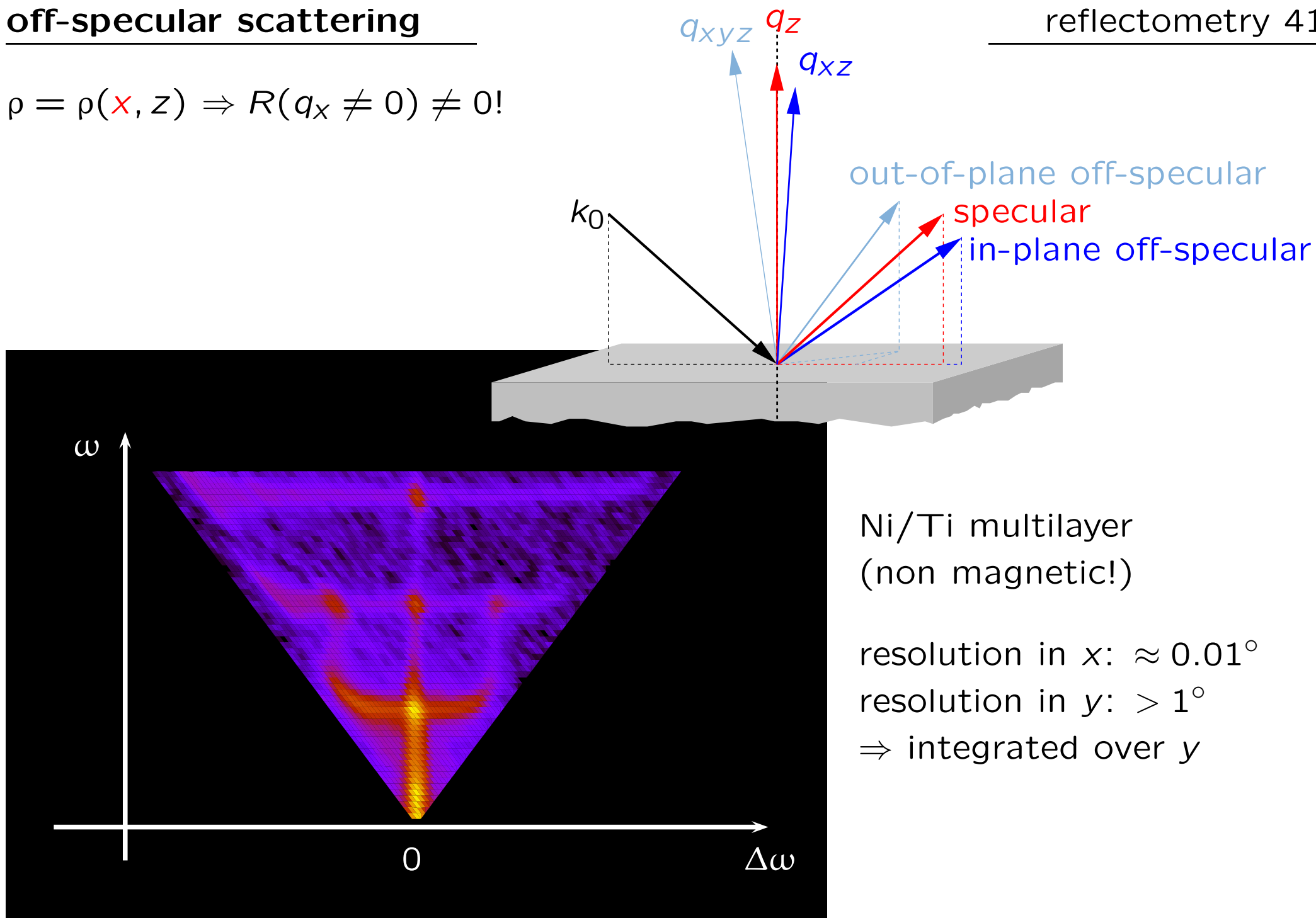
341 Å
non-functionalised

1016 Å
leucine functionalised

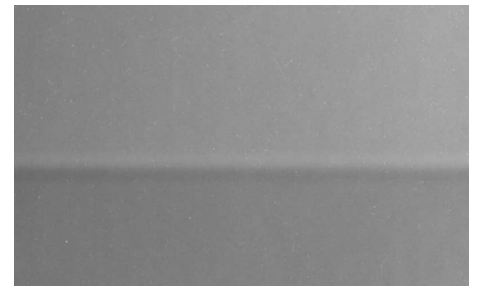
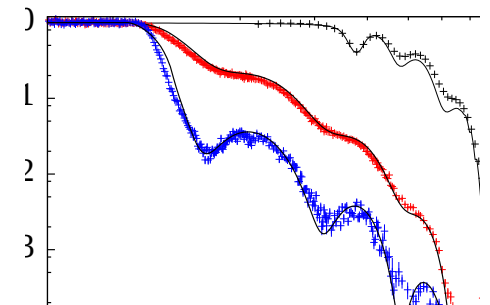
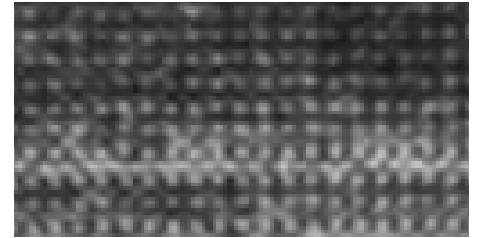
867 Å
serine functionalised



$$\rho = \rho(x, z) \Rightarrow R(q_x \neq 0) \neq 0!$$



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total reflection and refraction change beam direction

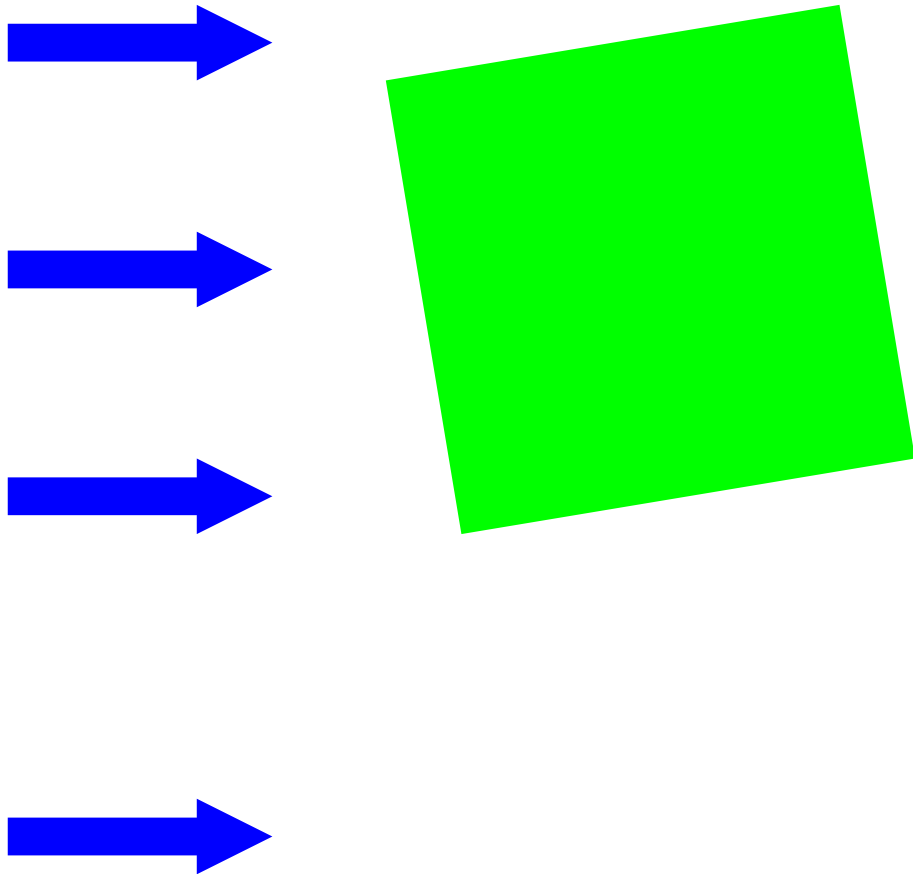
⇒ important for *large* sample-detector distances

also (optically) rough interfaces show significant total reflection!

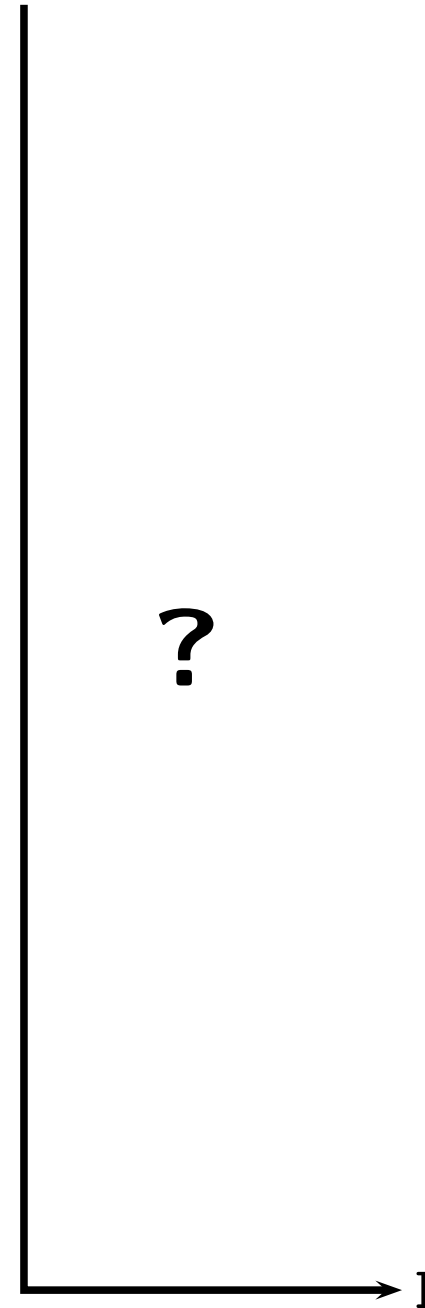
transmission of a slightly tilted square prism:

$n < 1 \Rightarrow$ total external reflection possible

parallel, monochromatic beam

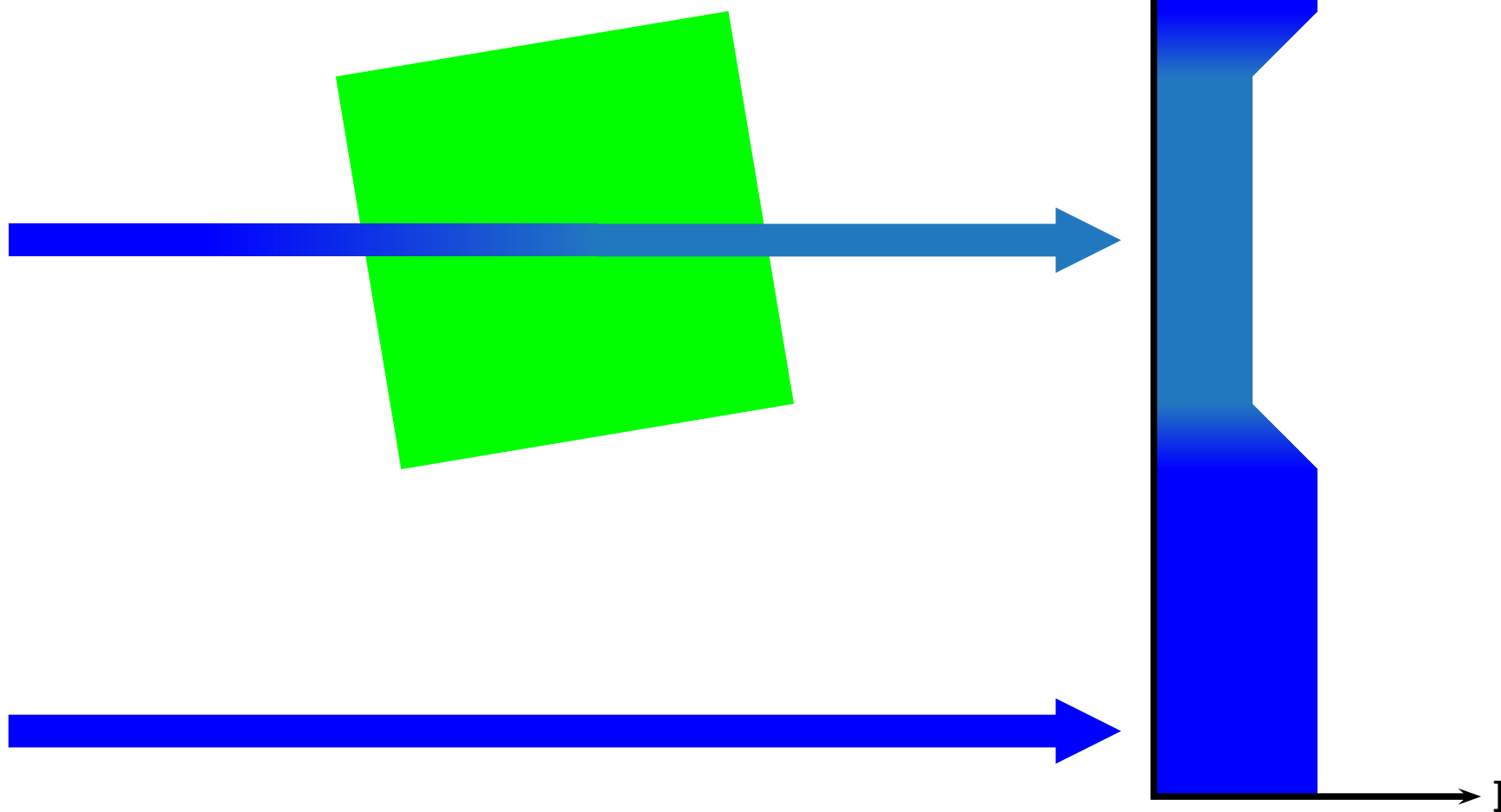


?



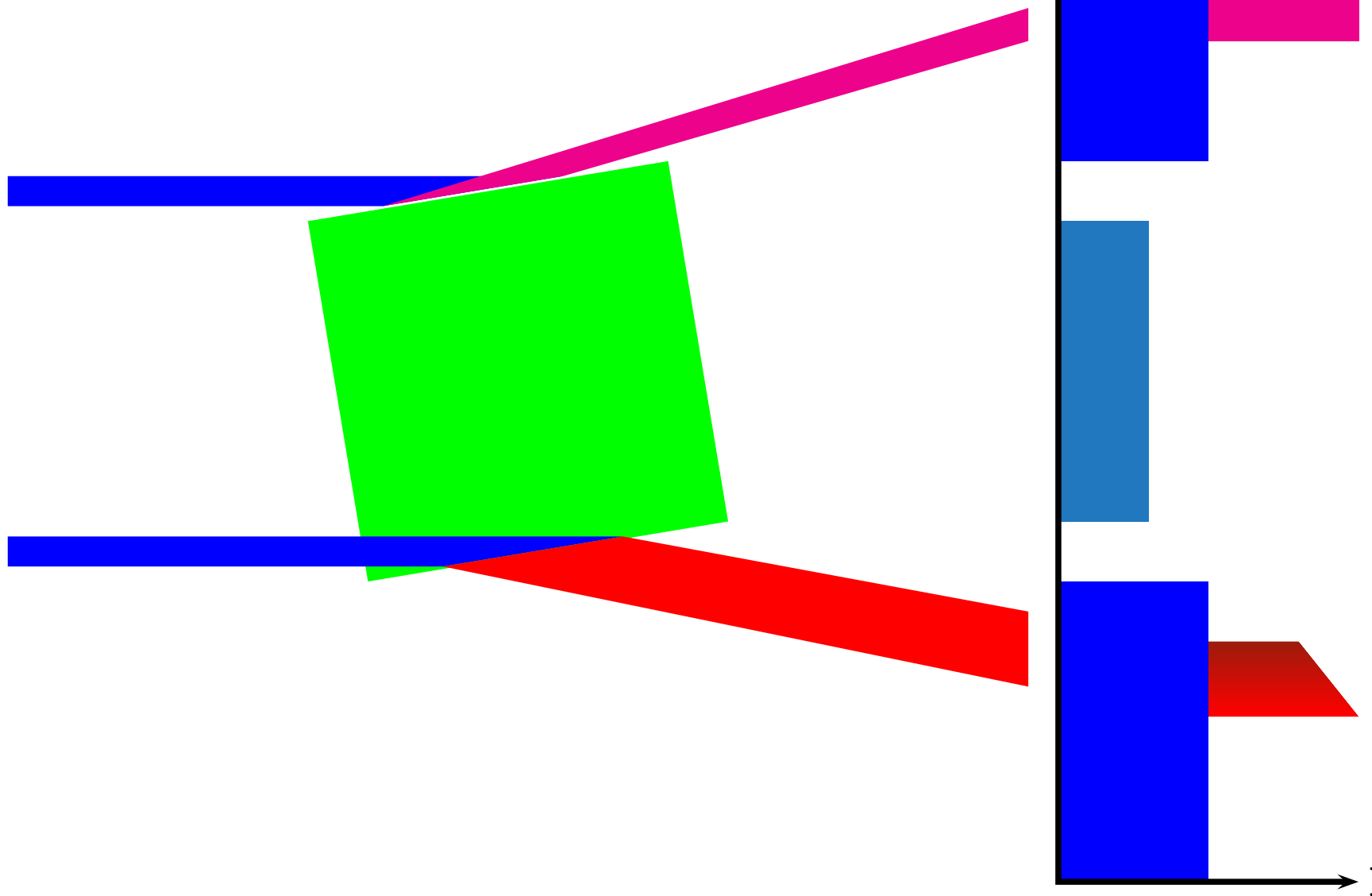
transmission of a slightly tilted square prism:

- no refraction
- no reflection



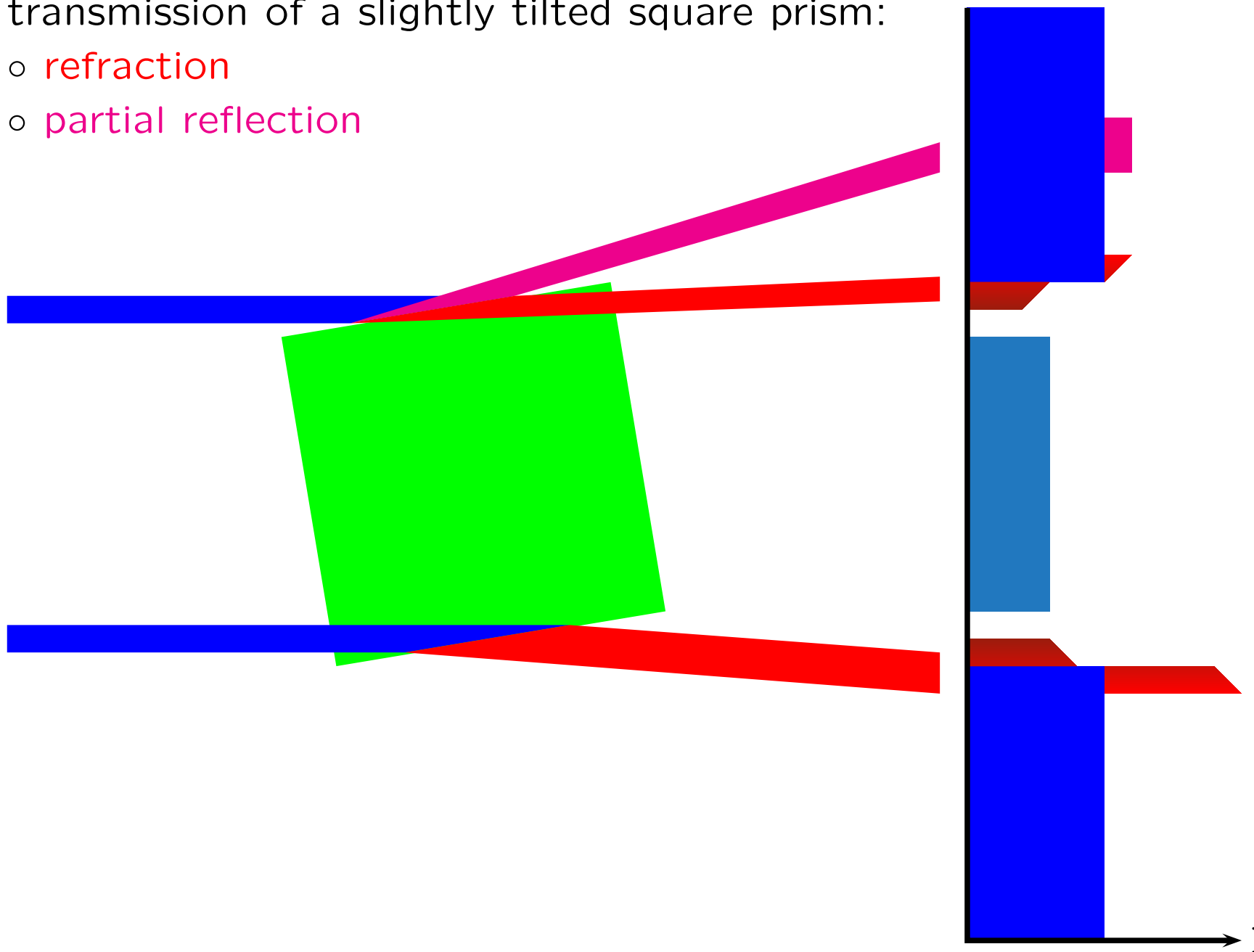
transmission of a slightly tilted square prism:

- refraction
- total reflection



transmission of a slightly tilted square prism:

- refraction
- partial reflection

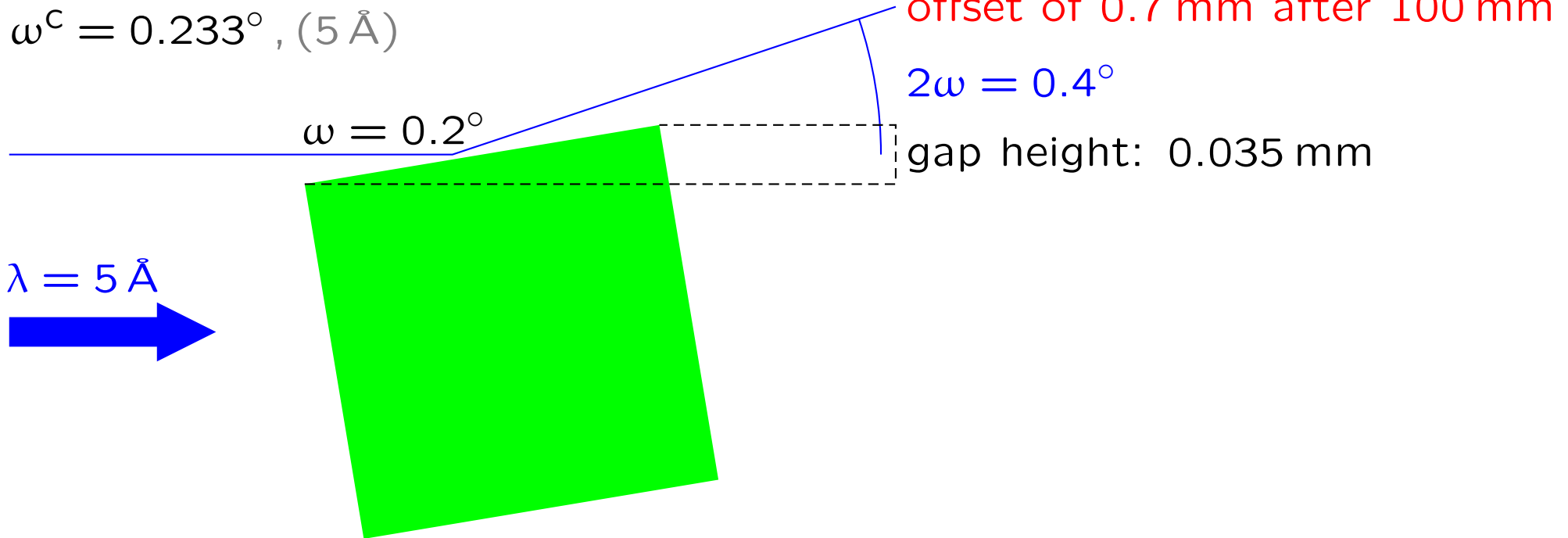


transmission of a slightly tilted square prism: some numbers

Al prism with $\varnothing = 10 \times 10 \text{ mm}^2$

$n = 1 - 8.3 \cdot 10^{-6}$, (5 Å)

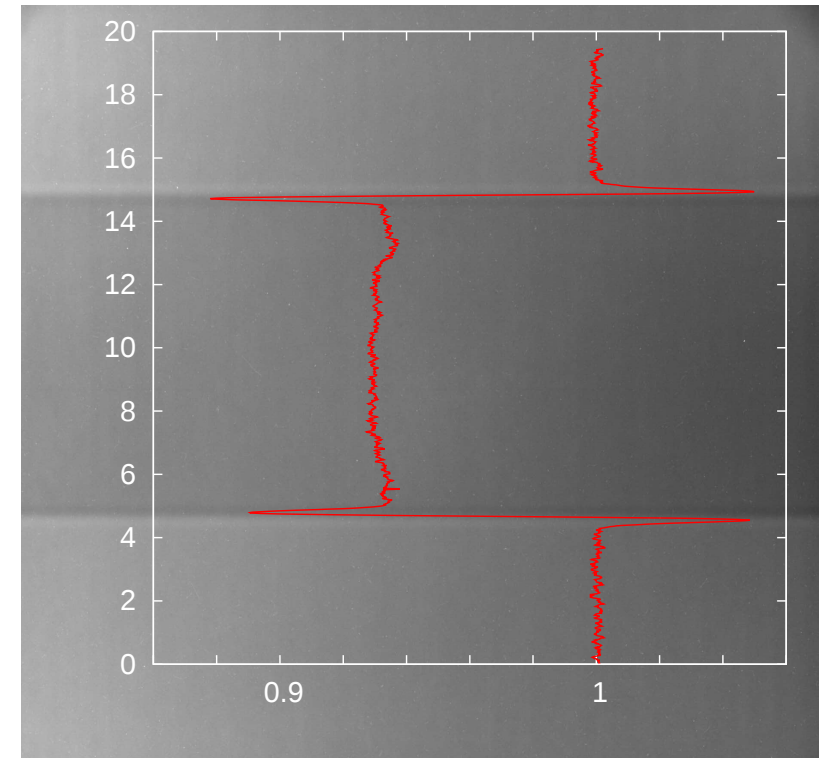
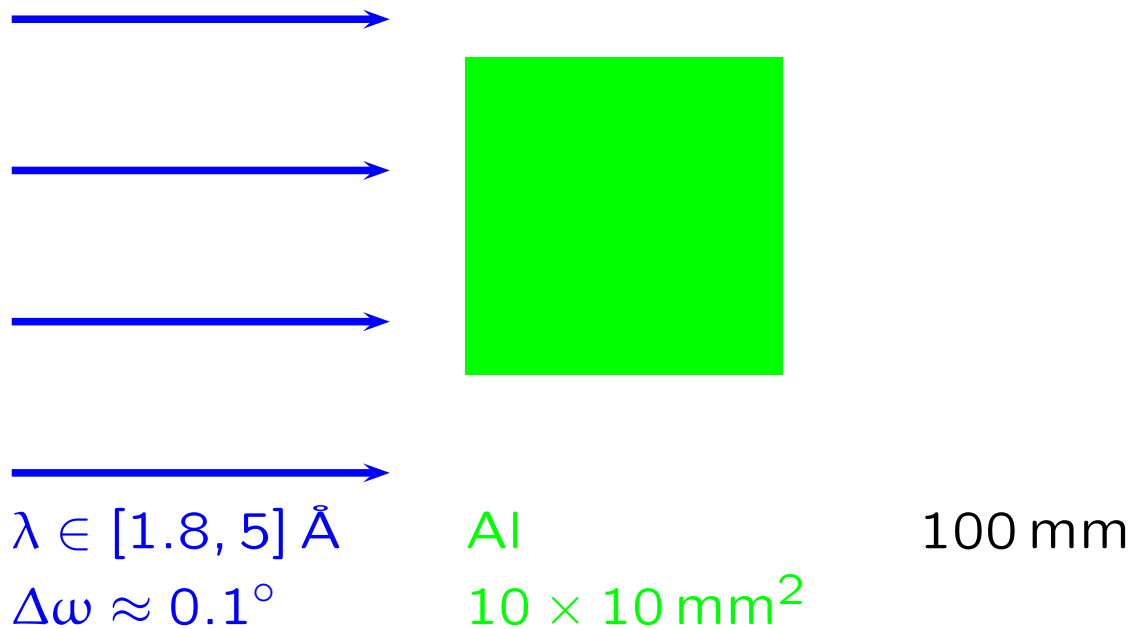
$\omega^c = 0.233^\circ$, (5 Å)



$\Rightarrow$ reflection (and refraction) can lead to detectable features

like *halos* or *shadows*

measured transmission (Eberhard Lehmann, PSI)

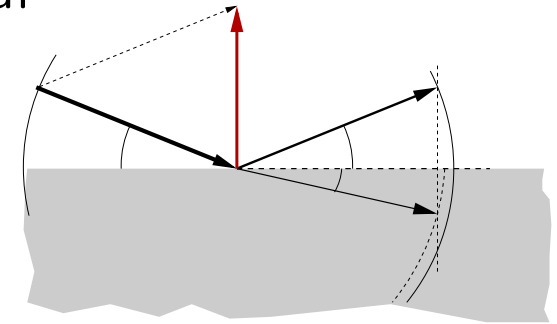


Al cube has not perfectly flat and parallel surfaces

$$\Rightarrow \omega = 0 \pm \Delta\omega_{\text{beam}} \pm \Delta\omega_{\text{surface}}$$

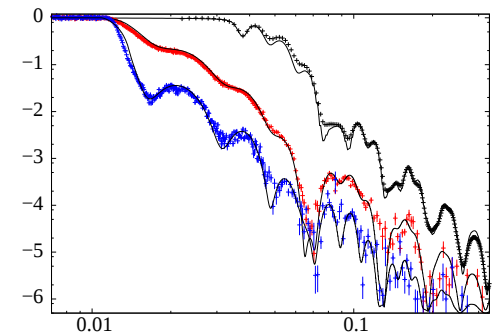
reflectometry

probes **depth-profile** of some potential
averages laterally
⇒ ideal for layered systems
data analysis by **modelling**



with neutrons

resolution: atom to sub- μm
isotope selective
detects **in-plane magnetic induction**



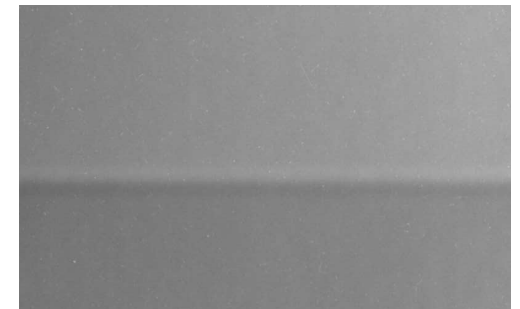
with x-rays

resolution: atom to sub- μm
detects electron density

... in resonance detects **magnetic states** of atoms

radiography

might be affected !!!



reflectometry, in general :

J. Daillant, A. Gibaud:

X-ray and Neutron Reflectivity

Lect. Notes Phys. 770 (Springer 2009)

U. Pietsch, V. Holý, T. Baumbach:

High-Resolution X-Ray Scattering

(Springer 2004)

... on magnetic systems

F. Ott:

Neutron scattering on magnetic surfaces

C. R. Physique **8**, 763-776 (2007)

... using resonant x-rays

S. Brück:

Magnetic Resonant Reflectometry on Exchange Bias Systems

Dissertation, Stuttgart 2009